# New Constructions of Optical codes, and Analysis for SAC OCDMA Systems 

Ph.D. Thesis

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# New Constructions of Optical codes, and Analysis for SAC - OCDMA Systems 

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Mrs. Soma Kumawat

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Dr. M. Ravi Kumar

Associate Professor
Place: Jaipur Date:

Dedicated to
My Family

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Mrs. Soma Kumawat

## List of Important Abbreviations

| 1D | One dimensional |
| :--- | :--- |
| 2D | Two dimensional |
| BBS | Broad Band Sources |
| BD | Balanced Detection |
| BER | Bit Error Rate |
| CDMA | Code Division Multiple Access |
| CW | Constant Weight |
| CL | Constant Length |
| DD | Direct Detection |
| DW | Double Weight |
| EDW | Eahanced Double Weight |
| FCC | Flexible Cross Correlation |
| FBG | Fiber Bragg Gratings |
| IPCC | In Phase Cross Correlation |
| KS | Khazani Syed |
| LED | Light Emitting Diodes |
| MAI | Multiple Access Interference |
| MDW | Modified Double Weight |
| MZM | Mach Zehnder Modulator |
| MQC | Modified Quadratic Congruence |
| MFH | Modified Frequency Hopping |
| MS code | Multi Service code |
| OCDMA | Optical Code Division Multiple Access |
| PDs | Photo Detector |
| PIIN | Phase Induced Intensity Noise |
| PSD | Power Spectral Density |


| QoS | Quality of Service |
| :--- | :--- |
| RD code | Random Diagonal code |
| SAC | Spectral Amplitude Coding |
| SNR | Signal to Noise Ratio |
| S/S | Spectral/Spatial |
| VW | Variable Weight |
| WDMA | Wavelength Division Multiple Access |
| ZCC | Zero Cross Correlation |
| ZCCC | Zero Cross Correlation Code |

## List of Important Symbols

| $d_{k}$ | Data bit of the $k$ th user <br> $e$ |
| :--- | :--- |
| electron charge |  |
| $G(v)$ | single sideband Power Spectral Density (PSD) of the <br> source |
| $\left(h v_{0}\right)$ | Photon energy |
| $h$ | Planck's constant |
| $I$ | Average photocurrent |
| $P_{s r}$ | Effective power of a broadband source at the receiver |
| $\left\langle I_{P I I N}^{2}\right\rangle$ | Phase-Induced Intensity Noise (PIIN) |
| $\left\langle I_{\text {shot }}^{2}\right\rangle$ | Shot noise |
| $\left\langle I_{\text {thermal }}^{2}\right\rangle$ | Thermal noise |
| $\tau_{c}$ | Coherence time |
| $v$ | Linewidth of broadband source |
| $\mathcal{R}$ | Responsivity |
| $K_{b}$ | Boltzmanns constant |
| $M$ | Basic matrix |
| $N_{B}$ | Number of users of basic matrix |
| $L_{B}$ | Code length of basic matrix |
| $\eta$ | Quantum efficiency |
| $T_{n}$ | Receiver noise temperature |
| $B$ | Electrical bandwidth |
| $R_{L}$ | Receiver Load resistor |
| $\lambda_{c}$ | IPCC |
| $L$ | Code length |
| $W$ | Code weight |
| $\lfloor x\rfloor$ | Floor $(\mathrm{x})$ |
| $\lceil x\rceil$ | Ceil(x) |

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Abstract

## Abstract

Spectral Amplitude Coding - Optical Code Division Multiple Access (SAC-OCDMA) systems are a type of OCDMA technique in which unique codes are mapped to different spectral lines of a broadband source. It eliminates the Multiple Access Interference (MAI) when codes with fixed In Phase Cross Corelation (IPCC) are used as address sequences. Double Weight (DW) codes are one of the code families reported for SAC-OCDMA systems. The property of these codes are that they have weight chips always in pairs. Due to that property, filtering requirements are reduced. These codes have ideal IPCC property. The code construction steps are easy to impelement. DW code structure is obtained only for weight two. The weight constraint inspires to develop codes with other weights. Modified Double Weight (MDW) code is also reported for even weights, greater than two. DW and MDW codes are limited to even weights. The code construction for odd weights greater than one is described and, that code is called Enhanced Double Weight (EDW) code. Khazani-Syed (KS) Code for even weights was constructed using combination of DW and MDW codes.

To generate a code for DW code family, first step is to construct a basic matrix. Depending on the number of users required in the code family, the basic matrix is repeated diagonally, known as mapping technique. Due to mapping, increment of code length is not constant. Even though mapping and crosscorrelation constraints are similar for all codes families of DW, they have different code construction algorithms, length and other properties. A generalised algorithm to construct these codes is a gap in literature which is investigated in this thesis with and without mapping.

A new generalized algorithm to construct EDW and MDW (PC1) like codes without mapping is proposed. The code construction is independent of mapping technique. Crosscorrelation value is equal to or less than 1 among all users. A single algorithm ( PC 1 ) is designed which provide the standardized formulation of code length, Signal to Noise Ratio ( $S N R$ ) and Bit Error Rate ( $B E R$ ) for all weight greater than 2. It (PC1) designs code for Constant Length (CL) and Constant Weight (CW). The numerical results using balanced detection and direct detection are obtained and compared.

The above proposed codes are developed for CL and CW which are not suitable for multimedia services. Variable Weight (VW) algorithm (PC2) is proposed
which is based on PC1. The cross correlation among all users is at most 1 . This code construction algorithm ensures higher power at receiver for higher weight users. Lower weight users receive less power compared to higher weight users. The difference in received power translates as varying performance, and are useful for multimedia applications.

The above proposed codes are constructed without using mapping technique. The effect of mapping and to construct the single code construction algorithms with mapping for all weights are proposed and analysed. Like DW code families, Basic matrix is first constructed using proposed algorithm. The number of users for basic code matrix depends on the code weight and on a constant value. As size of basic matrix is changed, $B E R$ and code length of users are changed. All above described codes are 1 Dimensional (1D) which have a limitation of fewer users due to finite bandwidth of source. To solve this problem, 2 Dimensional (2D) code construction is also proposed using proposed 1D code. 2D code gives better performance with higher cardinality compared to 1D code. Khazani-Syed (KS) Code for odd weights construction is also proposed.

MAI can be removed from SAC-OCDMA system by using electrical subtraction, but Phase Induced Intensity Noise (PIIN) still remains. All the above codes suffer from PIIN. A code design with zero cross correlation (ZCC) property removes the effect of MAI and suppress the effect of PIIN. The code with the property of ZCC is called as Zero Cross Correlation Code (ZCCC). The code structure of ZCCC does not have any overlapping of wavelengths between any users. A new code with zero cross correlation, termed as Zero Cross Correlation Code (ZCCC) is proposed without mapping. Code construction algorithm is designed with any weight for any number of users having constant, or variable weights. Variable weight (VW) codes give different quality of service, and are useful for multimedia applications.
Key Words - SAC-OCDMA, DW, MDW, EDW, MAI, IPCC, ZCCC.

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## Introduction and Review

### 1.1 Introduction

Optical networks provide the solution towards increased spectrum demand. The utilization of spectrum in proper and convenient manner is next raised question which is answered by different access techniques. They provide access and sharing of spectrum efficiently among different users. There are several access techniques such as Wavelength Division Multiple Access (WDMA) [1], Optical Time Division Multiple Access (OTDMA) [2], and Optical Code Division Multiple Access (OCDMA) [3, 4].

OCDMA has knocked the doors for future multiple access networks [3]. The basic concept of implementation of OCDMA is same as that of CDMA. The concept behind CDMA is to transmit the signature code in place of sending single one and same length zero sequences in place of sending single zero [5]. All the codes have same length but have unique pattern for different users. The patterns are defined according to chosen coding scheme. The au-

## C H A P T E R 1. introduction and review

tocorrelation function of a code gives a high peak. At receiver, a high peak is generated due to detection of desired code. On detection of a high peak, the receiver assumes the code was transmitted. OCDMA has many features such as; no need for centralized network control, number of codes decides the cardinality of a network, new user can easily be added to the networks, it does not require any scheduling, permitting asynchronous access with no waiting time, security against eavesdropping, supporting larger number of users, and provision for multimedia traffic. Therefore, OCDMA is a promising technology for next generation access network. On comparing with OTDMA and WDMA, where the transmission capacity can only be increased once, the total numbers of time or wavelength channels provide the capacity of system. On the other hand, OCDMA (at encoder fixed/variable) permits flexibility in capacity of system by generating codes to support network [6-9].

The performance of OCDMA systems is mainly affected by interference from other simultaneous users called Multi User Interference (MUI) or Multiple Access Interference (MAI) [10,11]. Spectral Amplitude Coding - OCDMA (SAC-OCDMA) systems are a type of the OCDMA technique in which unique codes are mapped to different spectral lines of a broadband source [12] [13]. It reduces the MAI when codes with fixed In Phase Cross Correlation (IPCC) are used as an address sequences. This reduction is realized by balanced detection of signals as shown in Figure 1.1. It also provides a low cost solution as it uses Broad Band Sources (BBS) like Light Emitting Diodes (LEDs).

### 1.2 Spectral Amplitude Coding (SAC) systems

Codes are represented as $\left(N, L, W, \lambda_{c}\right)$, where $N$ is number of users, $L$ is code length, $W$ is code weight and $\lambda_{c}$ is IPCC. Code length $(L)$ is total number of chips used by each user. Weight $(W)$ represents the number of chips having value equal to unity. The IPCC between two codes is defined as $\lambda_{c}=\sum_{j=1}^{L} a_{j} d_{j}$ for two users codes $A=\left(a_{1}, a_{2}, a_{3}, \ldots, a_{L}\right)$ and $D=$ $\left(d_{1}, d_{2}, d_{3}, \ldots, d_{L}\right)$ of code length $(L)$. When $\lambda_{c}=1$, it is considered that the code possesses ideal IPCC properties [14].

Figure 1.1 shows the block diagram of a SAC-OCDMA system. It employs transmitter and receiver pairs connected in a star configuration. The transmitter side incorporate light source, splitter, data generator, encoder, modulator and multiplexer. The light sources are BBS like LEDs and super luminescent diodes. The optical spectrum of BBS is divided into $L$ number of chips. These chips are allocated according to the signature codes. At the encoder for each user, the code is generated by selecting the wavelengths from optical spectrum of the BBS. These signals are modulated by Mach Zehnder Modulator (MZM) according to given data. As, when the data bit is 1 , chips are sent according to the signature code, and when the data bit is 0 , no pulse is launched from the BBS. Codes from different users are combined before they are launched onto the optical fiber. The main components of receiver are filtering components and photodiodes. At receiver for balanced detection (BD) technique, the received signal splits into two arms. The upper arm of decoder uses the same wavelength structure as that of the encoder. For lower arm of decoder, wavelength structure is selected in such a way that it eliminates the MAI. Signals from upper arm and lower arm are sent to an


Figure 1.1: Block diagram of SAC-OCDMA system using BD technique.
electrical subtractor to cancel out the MAI.
MAI is the main factor which degrades the performance, especially when numbers of users are large. For SAC-OCDMA, MAI is only determined by the values of IPCC $[15,16]$. One major advantage of such systems is that MAI can be eliminated when codes with fixed IPCC are used as address sequences. Nevertheless, such systems exhibit inherent PIIN (Phase-Induced Intensity Noise) due to spontaneous emission of the BBS that severely affects the overall system performance. To suppress the PIIN, the value of IPCC should be kept as small as possible [14]. Therefore, the codes with ideal IPCC become attractive. Many codes with ideal IPCC and other properties are reported for SAC-OCDMA systems.

### 1.3 Literature Survey

Spectral encoding is proposed using m-sequences codes in [12]. A single m-sequence code generates $N$ user codes, simply by cyclic shifting of the single code $N$ times. A $N \times N$ Hadamard matrix is used to generate codes

## C H A P T E R 1. introduction and review

for $(N-1)$ users [17]. The m-sequences and hadamard code are expressed as a $(L, W, \lambda)=(N,(N+1) / 2,(N+1) / 4)$ and $(N, N / 2, N / 4)$ respectively. These codes offer easy code construction, fixed IPCC and simple architecture. However, their performance is limited due to the large value of IPCC.

In [14] and [18], Modified quadratic congruence (MQC) $\left(P^{2}+1, P+1,1\right)$ code families based on quadratic congruence code are investigated, where $P$ is a prime number. However, there are only $P^{2}$ code sequences in a family with length $\left(P^{2}+P\right)$. MQC has a limitation in code section due to its dependence on prime number for $P$. Modified frequency hopping (MFH) $\left(Q^{2}+Q, Q+1,1\right)$ code families based on freguency hopping code is presented in [19], where $Q=p^{n}$ is a prime power. MFH code gives wider range in code selection on comparing with MQC code along with all its property. In [20], two algebraic construction methods for the balanced incomplete block design code are reported. In [21], three optical orthogonal codes construction are reported, based on mutually orthogonal latin squares or mutually orthogonal latin rectangles, integer lattice design and affine geometries. All these codes have algorithmic complexity such as projective geometry and block designs.

Partitioned partial prime codes are constructed using Kronecker Tensor product, multiplication operation, and matrix complement methods in [22]. Partitioned partial prime code family has low value of IPCC, flexible code length, and excellent orthogonality. Inspiteof these advantages, it has complex code construction, exists only for a prime number, and cross correlation calculation is time consuming. In [23], Diagonal permutation shifting code is proposed with fixed IPCC and short code length. It is constructed by using some simple algebraic ways and certain matrix operations. It has been derived from the prime code sequences based on Galois field. In [24] a code is reported with short code length named as Dynamic cyclic shift. It has

## C H A P T E R 1. introduction and review

cross correlation value between 1 and 0 . It consists of two parts- weight and dynamic parts. The weight part is designed using the value of weight. The dynamic part is a set of zeros. The weight sequence and dynamic sequence are clubbed together to form a code, and on cyclic shifting other code sequences are generated. The cardinality of this system is limited by the condition that the number of users must equal the code length. Diagonal eigenvalue unity (DEU) code is constructed for any integer value of weight in [25]. Jordan block matrix is used to design the DEU code. Four combinations are designed using weight (W) and number of users (N). The combination are (even, odd), (odd, even), (odd, odd) and (even, even). Cross correlation is less than or equal to one. DEU code has higher code length. SW-Matrix Partitioning is introduced in [26] and compared to DEU codes. It has shorter code length compared to DEU code.

In [27], an algorithm is reported as Fixed Right Shifting code based on modified Jordan block matrix with algebraic methods. It constructs the codes by using different combinations of even and odd values of number of users and weight. Its cross correlation $\lambda_{c} \leq 1$. Code length is defined as $L=N(W-2)+W$. The minimum code weight is 3 for code construction. Matrix partitioning code is reported in [28]. It used the Arithmetic Sequence to construct the codes. Arithmetic Sequence is a sequence in which the next term originates by adding a constant to its predecessor, and the difference of any two successive numbers is a constant. Cross correlation is smaller than or equal to one. Code length is defined as $N \times W / 2$. Any integer number of weight can be used in code construction. A Generalized Matrix Partitioning Code is reported which uses mathematical properties of matrix partitioning code in [29]. It defines the upper bounds and lower bounds for the code. By putting the value of $g$ (set of codes) equals to 1 , the matrix
partitioning code is generated. Crosscorrelation is one in the same group and zero with codes in different groups. It is constructed for all natural numbers. Code length is $L=\frac{g(W \times N)}{2}$. Double Weight codes are one of the code families constructed for SAC-OCDMA systems in [30]. The families includes the code construction of Double Weight (DW) [30], Modified Double Weight (MDW) [30], and Enhanced Double Weight (EDW) [31]. These codes have ideal IPCC property. The code construction steps are easy to implement. They have weight chips always in pairs which required less filtering component. Khazani-Syed (KS) Code for even weights was constructed in [32]. It is a combination of DW and MDW codes. Weight constraint with different algorithms are main difficult with these codes.

The Flexible Cross Correlation (FCC) codes are reported with property of flexible cross correlation. The code lengths are shorter for these codes which turn in higher cardinality. FCC eliminates the effect of MAI. Random Diagonal (RD) code is reported in [33]. Code construction is divided in two parts - code and data. At data part, it designs zero cross correlation code of weight 1. Code part consists of basics and weight parts. Weight part is responsible for increasing number of weights. It constructs code with shorter length. Cross correlation value is greater than zero and depends on weight and number of users. Code is designed for weight greater than 2. In [34], FCC Code is reported using tridiagonal code matrix. In [35], Sequential Algorithm code is reported with FCC property. It generates code set of any desired cross correlation properties with smallest code length for the given number of users. It used tridiagonal matrix code property to constructed code for any given number of users and weights. Drawback of FCC codes is higher value of cross correlation which leads to more PIIN. On the other hand, the codes constructed by FCC have shorter code length compared to
fixed cross correlation codes.
MAI can be removed from SAC-OCDMA system by using electrical subtraction, but PIIN still remains. Thus, PIIN can severely affect the overall system performance. All the above codes suffer from PIIN. The code design with zero cross correlation (ZCC) property removes the effect of MAI and suppresses the effect of PIIN.

The code with the property of zero cross correlation is called as Zero Cross Correlation Code (ZCCC). The code structure of ZCCC does not have any overlapping of wavelengths between any users. The ZCCC is reported with Constant Weight code construction in [36]. The ZCCC code construction along with LED Spectrum slicing is explained in [37]. These codes are using mapping technique to provide codes for higher number of users. Multi diagonal Code [38] and modified Zero Cross Correlation Code [39] are reported with ZCC property. The MAI is completely eliminated by using codes with ZCC property but at the price of longer code length. Longer code length requires wide band sources.

Enhanced Multi Diagonal code is invented in [40]. It improves the code property of multi diagonal and RD codes. It defined two matrices, data and code matrices as RD code. Data matrix is a diagonal matrix of size $N \times N$. It has zero cross correlation between all rows. Code matrix used chip combination (1 221 ) as DW code. This combination is repeated diagonally. Cross correlation of chip combination is 1 . Code length is $L=N+[N(W-$ $2)+1]$. Code is designed for weight greater than 2 .

All of the above described coding schemes have fixed code length and weight, and are not suitable for multimedia services. Thus, coding techniques with variable code weights and code lengths are required. The code weight indicates the amount of power sent by each code. Higher code weight

## C H A P T ER 1. INTRODUCTION AND REVIEW

means higher transmitted power and vice versa. Variable Weight (VW) optical orthogonal code to support multimedia services with different Quality of Service (QoS) was reported in [41]. VW Khazani Syed (KS) code was reported in [42]. KS code is designed only for even weights. It uses mapping technique to obtain codes for higher number of users for same weight and variable weight. Experimental and simulation results of VW KS code was done for SAC OCDMA system in [43]. In [44], hybrid fixed-dynamic weight assignment technique is reported for VW KS code. Comparison of various detection techniques for KS code is reported in [45]. VW Random Diagonal (RD) Code is reported in [46] for triple play service. RD code is designed for weights greater than 2. It uses two segments as code and data to obtain codes. Data segment has zero cross correlation. The code segment is responsible for cross correlation and its value is high. To obtain the codes for variable weight, RD code uses the mapping technique. A code construction is reported for Multi Service (MS) code in [47] for fixed weight, and variable QoS obtained by varying the number of codes in basic matrix.

All above described codes are 1 Dimensional (1D) which have a limitation of fewer users due to finite bandwidth of source. To solve this problem, Two Dimensional (2D) codes in Spectral/Spatial (S/S) domain have been reported. All the reported 2D codes extend the number of codes in spatial domain in which, each spectral component is split according to spatial code of that user.

The 2D M-matrices codes are reported in [48]. The performance of Mmatrices codes were affected by high value of cross correlation. To further increase the number of users along with performance and improve structure of system, Permuted M-matrices code was given in [49]. It used the cyclic property of Arrayed Waveguide Grating routers together with M-sequence
code. The permuted M-matrix code allowed a greater number of users [49]. The cross correlation value of 2D M-matrix codes is high resulting in inefficient performance. The 2D perfect difference codes were proposed in [50] to provide low cross correlation value. In [51], the 2D Diluted Perfect Difference codes were proposed to further increase performance of 2D PD codes. The DPD codes used the dilution method on the spectral and spatial codes. It has IPCC property. It reduces the effect of PIIN resulting in improved system performance along with number of users.

The Quadratic Congruence Code Matrices were constructed as 2D code in [52] with IPCC property to reduce MAI. In [53], the 2D Spatial division multiplexing-Balanced Incomplete Block Design codes were reported with spatial division multiplexing technique. The 2D Extended M Sequence/Extended Perfect Difference codes with a low IPCC value is given in [54]. Design of optical line terminal and optical network units were also described. Extended perfect difference code provided orthogonal property in spatial domain. The 2D hybrid codes also reported MAI cancellation property in [55]. The code has the property of spectral orthogonality. The spectral orthogonality was used to reduce the PIIN induced from the other users.

### 1.3.1 Motivation

OCDMA is promising technology for next generation access networks. Although, it has one major limitation, MAI. As the cardinality of system increases, MAI and Bit Error Rate $(B E R)$ increases. The MAI of system is removed and eliminated by using SAC-OCDMA systems [12, 15]. However, developing codes with good properties is a challenging task in the optical CDMA and SAC-OCDMA systems. To design a code with higher cardinality, better performance and less noise is an open task. The challenging
points in designing are; MAI increases as cardinality increases, PIIN and other noises increase the $B E R$, code to support various traffic demands, extension of codes in other dimensions. These points are motivating to develop code families for SAC-OCDMA systems.

The objective of the thesis can be stated as: To develop suitable codes for SAC-OCDMA system with desirable cross correlation properties, flexibility in implementation of algorithms, to support multimedia communication requirements, and efficient detection techniques. To simplify the system architectures to make it cheaper, and to improve the performance by reducing $B E R$.

### 1.4 Contributions

The overall contributions of the thesis can be summarized below.

- Proposed and analysed Generalized Optical Code construction for Enhanced and Modified Double Weight like Codes without mapping for SAC-OCDMA systems.
- Proposed and analysed variable weight code using Generalized Optical Code construction for Enhanced and Modified Double Weight like Codes for multimedia communication systems.
- Design of a new code construction for Double Weight (DW) code families for all weights with mapping.
- 2D code construction of a new algorithm for DW code families.
- Proposed code construction of Zero Cross Correlation Code (ZCCC) for constant weight and variable weight.
- Proposed 2D code design using existing DW code families.
- Proposed Khazani-Syed (KS) code design for odd weights.
- Analysis of different detection techniques.


### 1.5 Organization of the Thesis

The remainder of the thesis is organized as follows.
Chapter 2 describes the code construction algorithms reported for DW code families along with available work done in literature and followed with gaps in literature. An odd weight construction of KS code is also introduced in this chapter. It is followed with 2D code construction by using reported 1D DW codes.

Chapter 3 proposes the algorithm to construct generalized codes for Enhanced and Modified Double Weight like Codes without mapping for SACOCDMA systems. Constructed code is compared with reported EDW and MDW codes. It designs code for Constant Length (CL) and Constant Weight (CW). A single algorithm is implemented with standardized formulation of code length, $S N R$ and $B E R$ for all weights greater than 2.

A Variable Weight (VW) code construction algorithm is explained for generalized code in Chapter 4. Generalized code is explained in Chapter 3 for CL and CW. To obtain different $B E R$, VW algorithm is needed in which weight is varied. Variation of weights provides different $B E R$ for different services. It is designed for any number of users for weight greater than 2. It does not use mapping technique to obtain more users. The cross correlation value of atmost 1 is obtained between any two users. Code construction begins with the highest weight.

A new algorithm is developed for DW code families with mapping is presented in Chapter 5. A single code construction algorithm is proposed with mapping for all weights. It also has standardized formulation of code length, $S N R$ and $B E R$ for all weights. The major code construction steps are similar to DW code families like construct basic matrix and use mapping technique. It describes the effect of mapping on code performance. 2D code is also constructed by using 1D code construction. 2D code gives better performance with higher number of users compare to 1D code.

Chapter 6 proposes an algorithm to construct CW and VW codes with ZCC property. The constructed code is named as ZCCC. It does not use mapping technique to obtain codes for higher number of users. It eliminates the PIIN theoretically. Finally Chapter 7 summarizes the thesis with conclusions and future work.

# DW code families for <br> <br> SAC-OCDMA systems 

 <br> <br> SAC-OCDMA systems}

### 2.1 Introduction

Double weight (DW) code was first introduced by Aljunid et al. in [30] in 2004. It was proposed for constant weight 2 . It has simple and easy code construction along with ideal IPCC and shorter length. It also reduces the number of required filters due to number of chips occuring in pairs. Many advanced versions of this code have been reported resently. Evolution in DW code families from its introduction to persent is surveyed and presented in Section 2.2.

### 2.2 DW code families

### 2.2.1 1D codes

Code construction for 1 Dimensional (1D) codes for DW code families begin with constructing basic matrix $(M)$ of size $\left(N_{B} \times L_{B}\right)$ and weight $(W) . N_{B}$ and $L_{B}$ denotes number of users and code length for basic matrix. Number of users $\left(N_{B}\right)$ in basic matrix depends on particular code. Basic matrix is repeated diagonally to obtain number of users $(N)$. This method to obtain $N$ users code is known as mapping [30,31,56-58]. The cross correlation $\left(\lambda_{c}\right)$ is equal to 1 for users inside basic matrix $(M)$ and 0 for users outside basic matrix $(M)$.

DW code structure [30] is obtained only for weight two. The weight constraint inspires to develop codes with other weights. Modified Double Weight (MDW) code is also reported in [30] for even weights greater than two. It explains code design for $W=4$ only. For higher even weights construction, the chips combination of $(1,2,1)$ is kept for every three columns in $M$. Code construction steps are not outlined in [30] for MDW code. In [59], formulation of MDW code in terms of matrix is explained and described by using examples. In [60], generalised formulation is developed for MDW code without using matrix and mapping technique. A general equation is also given for code length calculation.

DW and MDW codes are limited to even weights. Code construction for odd weight greater than one is described in [31] and, the code is named as Enhanced Double Weight (EDW) code. Code construction steps are not outlined in [31] for EDW code. In $[61,62]$, formulation of EDW code in terms of matrix is explained and described by using examples. The reconstruction of EDW code is reported for higher weights in [61].

## Code Construction

## DW code

1. Construction of basic matrix $(M)$ using a fixed weight of 2 as described in [30] is shown below

$$
M=\left[\begin{array}{cccc}
1 & 1 & 0 & \text { Code 1 }  \tag{2.1}\\
0 & 1 & 1 & \text { Code 2 } \\
\hline 1 & 2 & 1 & \text { Sum }
\end{array}\right] .
$$

2. Chips follow ( $1,2,1$ ) patterns.
3. Mapping of $M$ to obtain $N$ users are done as

$$
\text { Mapping- : }\left[\begin{array}{cccc}
M & 0 & \ldots . . & 0  \tag{2.2}\\
0 & M & \ldots . . & 0 \\
. . & . . & . . & . . \\
0 & 0 & \ldots . . & M
\end{array}\right]_{N \times L}
$$

4. Code length is defined as $L=\left\{\begin{array}{cc}\frac{3 N}{2}, & \text { for } \mathrm{N} \text { is even } \\ \frac{3 N}{2}+\frac{1}{2}, & \text { for } \mathrm{N} \text { is odd }\end{array}\right.$

## MDW code

1. For MDW code using even weight greater than 2 , basic matrix is constructed as given in [59]

$$
M=\left[\begin{array}{ll}
A & B \\
C & D
\end{array}\right]
$$

where, $A$ consists of a zeros matrix of size $1 \times 3 \sum_{j=1}^{\frac{W}{2}-1} j, B$ is a matrix of size $1 \times 3\left(\frac{W}{2}\right)$ in which $Z_{2}$ is repeated $\left(\frac{W}{2}\right)$ times, $C$ is the basic
matrix for the next lower weight $(W-2)$, and $D$ is a matrix of size $\frac{W}{2} \times \frac{W}{2}$ expressed as:

$$
\left[\begin{array}{ccc}
0 & 0 & Z_{3} \\
0 & Z_{3} & 0 \\
Z_{3} & 0 & 0
\end{array}\right]
$$

where $Z_{1}=\left[\begin{array}{lll}0 & 0 & 0\end{array}\right] ; Z_{2}=\left[\begin{array}{lll}1 & 1 & 0\end{array}\right] ; Z_{3}=\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$. Chips follow the $(1,2,1)$ patterns.
2. Mapping is used to obtain $N$ users from basic matrix, as shown in Eq. (2.2).
3. Code length for $(W=4)$ is defined as

$$
L=(3 N)+\frac{8}{3}[\sin (N * 180) / 3]^{2} .
$$

## EDW code

1. For EDW code [62] using odd weight greater than 1 , basic matrix is constructed as

$$
M=\left[R_{1} R_{2} \ldots \ldots R_{W}\right]
$$

Where, $R$ is matrix of size $W \times \frac{\sum_{j=1}^{W} j}{W}$.
Each $R$ matrix has columns sum [2, 2 ... 1 ] in such a way sum 2 appear $\frac{W-1}{2}$ times. Chips follows the ( $2, . ., 2,1$ ) patterns.
2. To obtain $N$ users codes, mapping is used as explained in Eq. (2.2).
3. Code length $(W=3)$ is defined as

$$
L=(2 N)+\frac{8}{3}\left[\sin \frac{(N+1) 180}{3}\right]^{2} \frac{4}{3}\left[\sin \frac{N * 180}{3}\right]^{2}+\frac{4}{3} *\left[\sin \frac{(N+2) * 180}{3}\right]^{2} .
$$

Table 2.1: The comparison of DW code families

| Code | Existence | Weight | Size of $B_{M}$ | Code length $\left(L_{B}\right)$ |
| :---: | :---: | :---: | :---: | :---: |
| DW | 2 | 2 | $2 \times 3$ | 3 |
| MDW | even number $>2$ | even | $3 \times 9$ for $(W=4)$ | 9 for $(W=4)$ |
| EDW | odd number $>1$ | odd | $3 \times 6$ for $(W=3)$ | 6 for $(W=3)$ |

The other parameters for these codes are studied as: Performance of EDW code is analysed for multirate transmission in [62]. The system parameters for EDW code are examined by using Optisys 6.0 software. The parameters are number of users, fiber length, bit rate, spacing of chips and transmitted power in [63]. The point to multipoint Fiber to the home access network is designed for EDW code by using OptiSystem 7.0 software in [64]. In [65], Stimulated Brillouin Scattering effect is observed on system by using EDW code. MDW code performance is observed for multirate transmission in [66]. This technique was implemented in local area environment using ring network [67]. In [68], parallel and serial Fiber Bragg Gratings (FBG) constructions are used to set encoder and decoder structure using MDW code. EDW code performance is evaluated by using Direct Detection (DD) technique [56]. The AND detection technique for EDW code is simulated in [69]. The effect of Non Return to Zero and Return to Zero data format on $B E R$ using AND detection technique and MDW code is explained in [70]. A comparison between different detection techniques for EDW and MDW codes are presented in [71]. Single photo diode detection is proposed for EDW code in [72] and for MDW code in [73].

### 2.2.2 2D codes

1D code have a limitation of lower cardinality due limited bandwidth and $M A I$. To overcome the limitation, 1D code is extended to 2 Dimensions
(2D) code. 2D codes have combination of two algorithms, one applied in each dimension. The 2D code is developed from 1D MDW and 1D DW codes in [74], [75], [76] and [77]. In [76], the Avalanche Photo Diode is used to enhance the performance and cardinality. Due to PIIN reduction, cardinality of 2D code is improved compared to 1D code. Simulation results are shown in [75], [77]. The 2D code developed from 1D MDW and DW codes designed only for even weights. To resolve weight limitation, it is hybrid with others such as Flexible Cross Correlation in [78], [79]. In [80], 2D MDW code is simulated and compared for Non Return to Zero and Return to Zero data formats. The 2D code is developed by combining 1D EDW codes and Msequence codes in [81]. In [82], 2D Extended-EDW code is constructed by 1D EDW codes. The Time hopping Enhanced Double Weight is reported in [83] by merging EDW wavelength spreading into 2D time hopping scheme.

Literature gap -: These algorithms have different construction for different weights and varying calculation of code length, $S N R$ and $B E R$ with weight. Generalized algorithm is a gap in literature for all weights with standardized formulation of $B E R, S N R$ and code length.

### 2.3 New construction based on above codes

The section is divided into 2 subsections. Subsection 2.3.1 explains the code construction algorithm for KS code using odd and even weights. Subsection 2.3.2 describe the code construction algorithm for 2D code.

### 2.3.1 Odd weight construction for KS code

KS code construction is reported only for even weights. It is a combination of two code construction algorithms, MDW code and DW code. The odd
weight code construction for KS code is proposed. Proposed algorithm is a combination of previously proposed KS code (for even weight) and identity matrix. It designs the codes for all weights. Algorithm steps are-

- Choose weight [EVEN $\left(W_{E}\right) /$ ODD $\left.\left(W_{O}\right)\right]$.

1. If weight is even $W_{E}$.
(a) The first row of matrix is filled with $X$ from the left upto the number of ones equal to weight.
(b) The second row is filled with $Y$ diagonally, so column sum [1 $21]$ is obtained for every three columns.
(c) Fill all empty spaces with $Z$.
(d) Repeat steps a to c from second row, until all rows obtain number of ones equal to weight.

Where, $X=\left[\begin{array}{lll}1 & 1 & 0\end{array}\right], Y=\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$ and $Z=\left[\begin{array}{lll}0 & 0 & 0\end{array}\right]$.
2. Else, weight is odd $W_{O}$.
(a) Construct basic matrix $A$ of next smaller weight ( $W_{O}-1$ ).
(b) Construct identity matrix $B$ of size $B_{m} \times B_{m}$, where $B_{m}=$ $\left\lfloor\frac{W}{2}\right\rfloor+1$. Where $\lfloor x\rfloor$ is floor function.
(c) An identity matrix is concatenated with basic matrix of next smaller weight as

$$
\begin{equation*}
\text { Basic matrix }=[A \mid B] \tag{2.3}
\end{equation*}
$$

- Number of users $\left(N_{B}\right)$ in basic matrix is $\lfloor w / 2\rfloor+1$ for even and odd weights.
- Code lengths are defined as

For even weight,

$$
\begin{equation*}
L_{E}=3 \sum_{1}^{\lfloor W / 2\rfloor} i \tag{2.4}
\end{equation*}
$$

For odd weight,

$$
\begin{equation*}
L_{O}=3 \sum_{1}^{\lfloor W / 2\rfloor} i+\left\lfloor\frac{W}{2}\right\rfloor+1 \tag{2.5}
\end{equation*}
$$

- The basic matrix is repeated $\left\lceil N / N_{B}\right\rceil$ number of times, where $\lceil x\rceil$ is ceil function.
- Total code length is $L_{E}\left\lceil N / N_{B}\right\rceil$ and $L_{O}\left\lceil N / N_{B}\right\rceil$ for even and odd weights respectively.

Code construction example of weight 3 is as follows.

1. Weight is odd.
2. Number of users $N_{B}$ in basic matrix $B_{m}$ is $\lfloor W / 2\rfloor+1=2$.
3. First basic matrix of next lower weight is constructed.
4. Basic matrix of $(W-1)=2$ is constucted as
(a) The first row is filled with $X$.
(b) The second row is filled with $Y$.
(c) Basic matrix is

$$
B_{m_{E}}=\left[\begin{array}{lll}
1 & 1 & 0 \\
0 & 1 & 1
\end{array}\right]
$$

5. Construct identity matrix of size $B_{m} \times B_{m}$.
(a) $B_{m}=\left\lfloor\frac{W}{2}\right\rfloor+1=2$.
(b) Identity matrix of size $2 \times 2$ is

$$
B_{m_{O}}=\left[\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right]
$$

6. Attach both matrix as

$$
B_{m}=\left[\begin{array}{lllll}
1 & 1 & 0 & 1 & 0 \\
0 & 1 & 1 & 0 & 1
\end{array}\right]
$$

7. $L_{O}=3 \sum_{1}^{\lfloor W / 2\rfloor} i+\left\lfloor\frac{W}{2}\right\rfloor+1=5$.

## $B E R$ Anaysis

Figure 2.1 shows the block diagram of system setup for KS code. At the transmitter, the code sequences are generated by selecting wavelengths as per given code from Broadband Source (BBS). These selected wavelengths are modulated by MZM as per data. The output of each user is combined and sent to the optical fiber. At receiver, balanced detection technique is used to detect data. The received signal is divided into two parts, upper part and lower part. The upper part has same wavelength structure as an encoder. The wavelength structure of lower part of decoder is defined according to binary sum of columns. The output photodetector is sent to electrical subtractor to remove MAI.

Let the $j$ th component of the $k$ th proposed code is $H_{k}(j)$. The correlation function of upper part is given as

$$
\sum_{j=1}^{L} H_{k}(j) \cdot H_{l}(j)=\left\{\begin{array}{ccc}
W & k=l & \text { same user at basic matrix }  \tag{2.6}\\
1 & k \neq l & \text { other users at basic matrix } \\
0 & k \neq l & \text { other users outside basic matrix }
\end{array}\right.
$$

The cross-correlation function of lower part of decoder is obtained as


Figure 2.1: System block diagram of KS code for encoder and decoder.

1. Ex-ORing desired user with interfering user.

$$
H_{Z}(j)=\sum_{j=1}^{L} H_{k}(j) \oplus H_{l}(j)
$$

$\oplus$ denotes the Ex-OR function.
2. $H_{Z}$ is $A N D$ with given interfering user [57].

$$
H_{Y}(j)=H_{Z}(j) \cdot H_{l}(j)
$$

where • denotes the $A N D$ function.

$$
H_{Y}(j)=\left\{\begin{array}{ccc}
0 & k=l & \text { same user at basic matrix }  \tag{2.7}\\
(W-1) & k \neq l & \text { other users at basic matrix } \\
0 & k \neq l & \text { other users outside basic matrix }
\end{array}\right.
$$

3. Correlation function is given as

$$
\frac{\sum_{j=1}^{L} H_{k}(j) \cdot H_{Y}(j)}{(W-1)}=\left\{\begin{array}{ccc}
0 & k=l & \text { same user at basic matrix }  \tag{2.8}\\
1 & k \neq l & \text { other users at basic matrix } \\
0 & k \neq l & \text { other users outside basic matrix }
\end{array}\right.
$$

Photodiodes are used to detect optical power in upper and lower parts. Outputs of two photodiodes are sent to an electrical subtractor to cancel out MAI.

To analyse $B E R$ of the system, the Gaussian approximation with following assumptions [14], [18] are considered as.

- Each light source is ideally unpolarized and its spectrum is flat for given bandwidth $\left[v_{0}-\Delta v / 2, v_{0}+\Delta v / 2\right]$, where $v_{0}$ is the central optical frequency and $\Delta v$ is optical source bandwidth.
- Each bit stream is synchronized for each user.
- Spectral width of each frequency component is identical.
- The received power is the same for each user.

The above assumptions are used for mathematical simplification. At receiver, selected wavelengths from both parts are incident upon a photodetector, the phase noise of the fields causes an intensity noise term in the photo-detector output. The coherence time of a thermal source [18] is given by

$$
\begin{equation*}
\tau_{c}=\frac{\int_{0}^{\infty} G^{2}(v) d(v)}{\left[\int_{0}^{\infty} G(v) d(v)\right]^{2}} \tag{2.9}
\end{equation*}
$$

In the above equation, $G(v)$ is the single sideband Power Spectral Density (PSD) of the source $[25,57,58]$.

The variance of photocurrent due to the detection of an ideally unpolarized thermal light, which is generated by spontaneous emission, can be written as

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\left\langle I_{\text {shot }}^{2}\right\rangle+\left\langle I_{P I I N}^{2}\right\rangle+\left\langle I_{\text {thermal }}^{2}\right\rangle \tag{2.10}
\end{equation*}
$$

Where

- Phase-Induced Intensity Noise (PIIN) is

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=I^{2} B \tau_{c} . \tag{2.11}
\end{equation*}
$$

- Shot noise is

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e I B . \tag{2.12}
\end{equation*}
$$

- Thermal noise is

$$
\begin{equation*}
\left\langle I_{\text {thermal }}^{2}\right\rangle=\frac{4 K_{b} T_{n} B}{R_{L}} . \tag{2.13}
\end{equation*}
$$

The PSD of the received optical signals can be written as $[25,57,58]$ :

$$
\begin{equation*}
r(v)=\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) r e c(j) \tag{2.14}
\end{equation*}
$$

Where $d_{k}$ is the data bit of the $k$ th user, $P_{s r}$ is effective power of a broadband source at the receiver and $\operatorname{rec}(i)$ function in Eq.(2.14) is explained in terms of unit step function $u(v)$ as shown in Eqs. (2.15) and (2.16)

$$
\begin{equation*}
\operatorname{rec}(j)=u\left[v-v_{0}-\frac{\Delta v}{2 L}(-L+2 j-2)\right]-u\left[v-v_{0}-\frac{\Delta v}{2 L}(-L+2 j)\right] \tag{2.15}
\end{equation*}
$$

$$
\begin{equation*}
\operatorname{rec}(j)=u\left[\frac{\Delta v}{L}\right] \tag{2.16}
\end{equation*}
$$

At $P D_{1}$ of $k$ th receiver, total power is calculated as

$$
\begin{gather*}
P\left(P D_{1}\right)=\int_{0}^{\infty} G_{1}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} H_{k}(j) H_{l}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v \\
=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} H_{k}(j) H_{l}(j) \tag{2.17}
\end{gather*}
$$

Using correlation function from Eq. (2.6), Eq. (2.17) is written as

$$
\begin{equation*}
P\left(P D_{1}\right)=\frac{P_{s r} W}{L}+\frac{P_{s r}}{L} \sum_{k=1, k \neq p}^{N_{B}} d_{k} . \tag{2.18}
\end{equation*}
$$

At $P D_{2}$ of $k$ th receiver, total power is calculated as

$$
\begin{align*}
P\left(P D_{2}\right)=\int_{0}^{\infty} G_{2}(v) d v & =\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} H_{k}(j) H_{l}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v \\
P\left(P D_{2}\right) & =\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} H_{k}(j) H_{k}(j) \tag{2.19}
\end{align*}
$$

Using correlation property given in Eq. (2.8), Eq. (2.19) leads to

$$
\begin{equation*}
P\left(P D_{2}\right)=\frac{P_{s r}}{L} \sum_{k=1, k \neq p}^{N_{B}} d_{k} \tag{2.20}
\end{equation*}
$$

The received signal is the difference between photocurrents, which is expressed as $I=I_{1}-I_{2} . I_{1}$ and $I_{2}$ are currents at photodiodes.

$$
\begin{equation*}
I=\mathcal{R} P\left(P D_{1}\right)-\mathcal{R} P\left(P D_{2}\right) \tag{2.21}
\end{equation*}
$$

Here $\mathcal{R}=\eta e /\left(h v_{0}\right)$ is the responsivity as given in [18], and $\eta$ is the quantum efficiency of photodiode. $e$ is the electron's charge, and $\left(h v_{0}\right)$ is the photon energy, where $h$ is Planck's constant.

Replacing the values of $P\left(P D_{1}\right)$ and $P\left(P D_{2}\right)$ of total power incident at input of $P D_{1}$ and $P D_{2}$ from Eqs. (2.18) and (2.20) into Eq. (2.21), the recevied signal is

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r} W}{L} \tag{2.22}
\end{equation*}
$$

The shot noise is

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e B\left(I_{1}+I_{2}\right)=2 e B \mathcal{R}\left[P\left(P D_{1}\right)+P\left(P D_{2}\right)\right] \tag{2.23}
\end{equation*}
$$

Eqs. (2.18) and (2.20) are substituted in Eq. (2.23).

$$
\begin{equation*}
\left\langle I_{s h o t}^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}\left(W+2\left(N_{B}-1\right)\right)}{L} \tag{2.24}
\end{equation*}
$$

The approximation is used $\sum_{k=1}^{N} H_{k}(j) \approx \frac{N W}{L}$ as given in [18]. The PIIN is

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=B I_{1}^{2} \tau_{c 1}+B I_{2}^{2} \tau_{c 2}=B \mathcal{R}^{2}\left[\int_{0}^{\infty} G_{1}^{2}(v) d v+\int_{0}^{\infty} G_{2}^{2}(v) d v\right] \tag{2.25}
\end{equation*}
$$

Eqs. (2.18) and (2.20) are substituted in Eq. (2.25), PIIN is

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2} N W}{L^{2} \Delta v}\left[W+2\left(N_{B}-1\right)\right] \tag{2.26}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ as given in Eq. (2.10) is expressed as

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}\left(W+2\left(N_{B}-1\right)\right)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W\left(W+2\left(N_{B}-1\right)\right)}{L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}} . \tag{2.27}
\end{equation*}
$$

The probability of sending bit 1 is half, Eq. (2.27) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{P_{s r} e B \mathcal{R}\left(W+2\left(N_{B}-1\right)\right)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W\left[W+2\left(N_{B}-1\right)\right]}{2 L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{2.28}
\end{equation*}
$$

The Signal to Noise Ratio ( $S N R$ ), as defined in $[14,18,25,30,31,56-58$, 84, 85], of SAC-OCDMA systems can be written as

$$
\begin{equation*}
S N R=(I)^{2} /\left\langle I^{2}\right\rangle . \tag{2.29}
\end{equation*}
$$

Put values from Eqs. (2.22) and (2.28) in Eq. (2.29), $S N R$ is

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s r} W}{L}\right)^{2}}{\frac{P_{s r} e B \mathcal{R}\left(W+2\left(N_{B}-1\right)\right)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W\left[W+2\left(N_{B}-1\right)\right]}{2 L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}}} . \tag{2.30}
\end{equation*}
$$

The $B E R$ is calculated by using Gaussian approximation from $S N R$ as given in

$$
\begin{equation*}
B E R=\frac{1}{2} \operatorname{erfc} \sqrt{(S N R / 8)} \tag{2.31}
\end{equation*}
$$

## Numerical Results



Figure 2.2: $B E R$ versus number of users.
Comparison of KS code $(\mathrm{W}=3)$, MDW code $(\mathrm{W}=4)$ and EDW code $(\mathrm{W}=3)$.
Figure 2.3: $B E R$ versus code length.

Table 2.2: The Parameters used for $B E R$ calculation

| Parameter | Value |
| :---: | :---: |
| Linewidth of broadband source $(\Delta v)$ | 3.75 THz |
| Electrical bandwidth $(\mathrm{B})$ | 311 MHz |
| Broadband effective power $\left(P_{s r}\right)$ | -10 dBm |
| Quantum efficiency $(\eta)$ | 0.6 |
| Operating wavelength $\left(\lambda_{0}\right)$ | 1550 nm |
| Receiver noise temperature | 300 K |
| Receiver Load resistor | $1030 \Omega$ |
| Electron charge $(e)$ | $1.6 \times 10^{-19} \mathrm{C}$ |
| Planck's constant $(\mathrm{h})$ | $6.66 \times 10^{-34} \mathrm{~J} / \mathrm{s}$ |
| Boltzmann's constant $\left(K_{b}\right)$ | $1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}$ |

The relevant parameters used for numerical analysis, are listed in Table 2.2. Figure 2.2 is plotted for the $B E R$ versus number of users. It compare the $B E R$ for different codes, EDW $(W=3)$, MDW $(W=4)$ and KS code $(W=3)$ at a data rate of 622 Mbps using balanced detection. At $B E R$ of $10^{-12}$, number of users are 25,47 and 50 respectively for EDW code, KS code and MDW code. The variation of results for same weights are due to difference in code length. Required code length for KS code and EDW code are 250 and 200 respectively at 100 number of users as shown in Fig. 2.3. KS code gives improve performance with greater code length. But it give comparable performance with MDW code. KS code gives less $B E R$ with shorter length and less weight.

### 2.3.2 Proposed 2D code construction from DW code families

2D code construction is proposed using 1D DW code families which includes all weights. To construct 2D code, different combination of codes are used such as DW/DW, DW/EDW, DW/MDW, EDW/MDW, EDW/EDW,

MDW/MDW. Proposed 2D code is represented as $C_{g h}$ where $g$ and $h$ denotes the number of codes used in spectral and spatial domain respectively. $C_{g h}$ is given as $X_{g}^{T} Y_{h}$. Where $X_{g}$ and $Y_{h}$ are 1D codes represented as $X_{g}=x_{0}, x_{1}, x_{2}, \ldots \ldots, x_{\left(L_{x}-1\right)}$ and $Y_{h}=y_{0}, y_{1}, y_{2}, \ldots . ., y_{\left(L_{y}-1\right)}$. Where, $L_{x}$ and $L_{y}$ are code lengths of 1D code. Code weights are represented as $W_{x}$ and $W_{y}$ for $X_{g}$ and $Y_{h}$ respectively. The cross correlation is defined as

$$
\begin{equation*}
R_{g h}^{(d)}=\sum_{i=o}^{L_{x}-1} \sum_{j=0}^{L y-1} C^{(d)} C_{g h} . \tag{2.32}
\end{equation*}
$$

Where $C^{(d)}$ is denoted as characteristic matrices $d(0,1,2,3)$,

$$
C^{(0)}=X_{g}^{T} Y_{h}, C^{(1)}=\overline{X_{g}^{T}} Y_{h}, C^{(2)}=X_{g}^{T} \overline{Y_{h}}, \text { and } C^{(3)}=\overline{X_{g}^{T}} \overline{Y_{h}} . \text { Here }
$$ $X_{g}^{T}$ is transpose function of $X_{g} . \overline{X_{g}^{T}}$ and $\overline{Y_{h}}$ are complements of $X_{g}^{T}$ and $Y_{h}$ respectively.

The MAI elimination is obtained using Table 2.5 as follows

$$
\begin{align*}
R_{g, h}^{(0)}-\frac{R_{g, h}^{(1)}}{\left(W_{y}-1\right)}- & \frac{R_{g, h}^{(2)}}{\left(W_{x}-1\right)}+\frac{R_{g, h}^{(3)}}{\left(W_{x}-1\right)\left(W_{y}-1\right)} \\
& =\left\{\begin{array}{cc}
K_{x} K_{y} & \text { same user or } g=0, h=0 \\
0 & \text { other users of same basic matrix } \\
0 & \text { other users of other basic matrix }
\end{array}\right. \tag{2.33}
\end{align*}
$$

Due to mapping technique, the interfering users belong to their own basic matrix users. From other users, they have no interferences. $N_{B_{g}}$ and $N_{B_{h}}$ represent number of users in basic matrix.

## Performance analysis of code

The variance of photocurrent [24] can be written as given in Eq. (2.10). As in [54], [51], and Section 2.3.1, the Gaussian approximation is applied to

Table 2.3: 2D code construc- Table 2.4: 2D code construction using DW tion using DW codes.

|  | $\left[\begin{array}{llllll}1 & 1 & ] & {\left[\begin{array}{ll}1 & 1\end{array}\right]} \\ \hline 1 & 1 & 1 & 0 & 0 & 1\end{array}\right]$ |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 0 | 0 | 0 | 1 | 1 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| 1 | 1 | 1 | 0 | 0 | 1 | 1 |  |
| 1 | 1 | 1 | 0 | 0 | 1 | 1 |  | and EDW codes.

$\left.\begin{array}{|l|llllll|llllll|llllll|}\hline & {\left[\begin{array}{llllllllll} & 0 & 1 & 1 & 0 & 1\end{array}\right]} & {\left[\begin{array}{llllllll}1 & 1 & 0 & 0 & 1 & 1\end{array}\right]} & {[1} & 1 & 0 & 1 & 0 & 0\end{array}\right]$

Table 2.5: Cross correlation values for 2D code.

|  | $R^{(0)}(g, h)$ | $R^{(1)}(g, h)$ | $R^{(2)}(g, h)$ | $R^{(3)}(g, h)$ |
| :---: | :---: | :---: | :---: | :---: |
| $g=0 \bigcap h=0$ | $K_{x} K_{y}$ | 0 | 0 | 0 |
| $g=0 \bigcap h \neq 0$ | $W_{x}$ | $W_{x}\left(W_{y}-1\right)$ | 0 | 0 |
| $g \neq 0 \bigcap h=0$ | $W_{y}$ | 0 | $W_{y}\left(W_{x}-1\right)$ | 0 |
| $g \neq 0 \bigcap h \neq 0$ | 1 | $\left(W_{y}-1\right)$ | $\left(W_{x}-1\right)$ | $\left(W_{x}-1\right)\left(W_{y}-1\right)$ |

system. The PSD of the received optical signals can be written as

$$
\begin{equation*}
r(f)=\frac{P_{s r}}{W_{y} \Delta f} \sum_{U=1}^{U} d(u) \sum_{i=0}^{\left(L_{x}-1\right)} \sum_{j=0}^{\left(L_{y}-1\right)} a_{i j}(u) F(f, i) \tag{2.34}
\end{equation*}
$$

Here $d(u)$ is the data bit of the $u$ th user, $P_{s r}$ is effective power of a BBS at the receiver, $a_{i, j}(u)$ is element of $u$ th user code and $F(f, i)$ function in Eq.(2.34) is explained in terms of unit step function $u(f)$ as shown in Eqs.(2.35).

$$
\begin{equation*}
F(f, i)=u\left[f-f_{0}-\frac{\Delta f}{2 L_{x}}\left(-L_{x}+2 i\right)\right]-u\left[f-f_{0}-\frac{\Delta f}{2 L_{x}}\left(-L_{x}+2 i+2\right)\right] \tag{2.35}
\end{equation*}
$$

PSDs of optical signals at PDs of the receiver can be written as

$$
\begin{array}{r}
S_{0}(f)=\frac{P_{s r}}{W_{y} \Delta f} \sum_{u=0}^{U} d(u) \sum_{i=0}^{L_{x}-1} \sum_{j=0}^{L_{y}-1} a_{i j}^{(0)} a_{i j}(u) F(f, i) \\
S_{1}(f)=\frac{P_{s r}}{W_{y}\left(W_{y}-1\right) \Delta f} \sum_{u=0}^{U} d(u) \sum_{i=0}^{L_{x}-1} \sum_{j=0}^{L_{y}-1} a_{i j}^{(1)} a_{i j}(u) F(f, i) \\
S_{2}(f)=\frac{P_{s r}}{W_{y}\left(W_{x}-1\right) \Delta f} \sum_{u=0}^{U} d(u) \sum_{i=0}^{L_{x}-1} \sum_{j=0}^{L_{y}-1} a_{i j}^{(2)} a_{i j}(u) F(f, i) \\
S_{3}(f)=\frac{P_{s r}}{W_{y}\left(W_{x}-1\right)\left(W_{y}-1\right) \Delta f} \sum_{u=0}^{U} d(u) \sum_{i=0}^{L_{x}-1} \sum_{j=0}^{L_{y}-1} a_{i j}^{(3)} a_{i j}(u) F(f, i) \tag{2.39}
\end{array}
$$

Using Table 2.5, The effect of MAI is split into three parts, i.e., $g=$ $0 \bigcap h \neq 0, g \neq 0 \bigcap h=0$ and $g \neq 0 \bigcap h \neq 0$. The interfering users for these parts are $\left(N_{B_{h}}-1\right),\left(N_{B_{g}}-1\right)$, and $\left(N_{B_{h}}-1\right) \times\left(N_{B_{g}}-1\right)$ respectively. The ensemble average of the interference amount for three groups are as

$$
\begin{gather*}
A_{1}=\frac{(U-1)\left(N_{B_{h}}-1\right)}{g h-1}  \tag{2.40}\\
A_{2}=\frac{(U-1)\left(N_{B_{g}}-1\right)}{g h-1}  \tag{2.41}\\
A_{3}=\frac{(U-1)\left(N_{B_{h}}-1\right)\left(N_{B_{g}}-1\right)}{g h-1} \tag{2.42}
\end{gather*}
$$

Set $d(u)=1$ for worst case analysis [55] and use PSDs of PDs to calculate the output currents of each PDs as

$$
\begin{equation*}
I_{0}=\mathcal{R} \int_{0}^{\infty} S_{0}(f) d f \tag{2.43}
\end{equation*}
$$

$$
\begin{gather*}
I_{0}=\frac{\mathcal{R} P_{s r}}{W_{y} L_{x}}\left[K_{x} K_{Y}+\frac{W_{x}(U-1)\left(N_{B_{h}}-1\right)}{g h-1}\right. \\
\left.+\frac{W_{y}(U-1)\left(N_{B_{g}}-1\right)}{g h-1}+\frac{(U-1)\left(N_{B_{h}}-1\right)\left(N_{B_{g}}-1\right)}{g h-1}\right]  \tag{2.44}\\
I_{1}=\mathcal{R} \int_{0}^{\infty} S_{1}(f) d f  \tag{2.45}\\
I_{1}=\frac{\mathcal{R} P_{s r}}{W_{y} L_{x}}\left[\frac{W_{x}(U-1)\left(N_{B_{h}}-1\right)}{g h-1}+\frac{(U-1)\left(N_{B_{h}}-1\right)\left(N_{B_{g}}-1\right)}{g h-1}\right]  \tag{2.46}\\
I_{2}=\mathcal{R} \int_{0}^{\infty} S_{2}(f) d f  \tag{2.47}\\
I_{2}=\frac{\mathcal{R} P_{s r}}{W_{y} L_{x}}\left[\frac{W_{y}(U-1)\left(N_{B_{g}}-1\right)}{g h-1}+\frac{(U-1)\left(N_{B_{h}}-1\right)\left(N_{B_{g}}-1\right)}{g h-1}\right]  \tag{2.48}\\
I_{3}=\mathcal{R} \int_{0}^{\infty} S_{3}(f) d f \tag{2.49}
\end{gather*}
$$

The average output photocurrent of the receiver is

$$
\begin{equation*}
I=I_{0}+I_{1}+I_{2}+I_{3}=\frac{\mathcal{R} P_{s r} W_{x}}{L_{x}} \tag{2.51}
\end{equation*}
$$

The shot noise is written as

$$
\begin{equation*}
I_{\text {shot }}=2 e B\left(I_{0}+I_{1}+I_{2}+I_{3}\right) \tag{2.52}
\end{equation*}
$$

The PIIN is given as

$$
\begin{equation*}
I_{P I I N}=\frac{B L x}{2 v}\left(\left(I_{0}-I_{2}\right)^{2}+\left(I_{1}-I_{3}\right)^{2}\right) \tag{2.53}
\end{equation*}
$$



Figure 2.4: $B E R$ is compared for different value of $g$ and $h$ for proposed 2D code.

The $S N R$ is calculated as per written in Eq. (2.29), and $B E R$ from $S N R$ is expressed as given in Eq. (2.31).

## Numerical Results

2D code reduces PIIN which turns to reduce $B E R$, and increases cardinality. Because of that Electrical bandwidth (B) of system set to 1024 M Hz results are shown and compared at $10^{-9}$ and $10^{-12}$. Figure 2.4 depicts the affect of varying number of codes at spectral and spatial dimension on $B E R$. The weight of the code is set to value $W_{x}=2, W_{y}=2$. The total number of users is chosen to be 300 . The number of codes for both dimension are taken as $(g=20, h=15),(g=15, h=20)$, and $(g=10, h=30)$. At BER of $10^{-12}$, number of users obtained are 17, 111 and 270 for codes ( $g=20, h=15$ ), $(g=15, h=20)$, and $(g=10, h=30)$ respectively. As the value of spatial codes $h$ is increased and spectral codes $g$ is decreased, $B E R$ performance is improved. Numerical result shows that $B E R$ is decreased as $h$ is maximized and $g$ is minimized.

### 2.4 Summary

A survey on Double Weight code families is presented. The DW code family is one of the code families proposed for SAC-OCDMA systems to reduce MAI. These codes have ideal IPCC property. Code construction steps are easy to implement. They have weight chips always in pairs which reduce number of filtering element. Odd weight implementation of KS code is also introduced in chapter. 2D code construction using DW code families are also introduced. However, DW codes family have different constructions of basic matrix, generalised formulation of code length and $B E R$ is not presented, and have limitation of weight.

# Generalized Optical Code construction for Enhanced and Modified Double Weight like Codes without mapping 

### 3.1 Introduction

To generate a code for DW code family, first step is to construct a basic matrix. Depending on the number of users required in the code family, the basic matrix is repeated diagonally, known as mapping technique. Due to mapping, increment of code length is not constant. Its increment is dependent on the size of basic matrix and required number of additional users. For example, if basic matrix has size $(3 \times 9)$ where users are 3 and code length is 9 . For 3 additional users, code length becomes 18. Even though mapping
and crosscorrelation constraints are similar for all codes families of DW, they have different code construction algorithms, length and other properties. A generalised algorithm to construct these codes is a gap in literature which is investigated in Chapters 3, 4 and 5, with and without mapping.

A new generalized algorithm to construct EDW and MDW like codes without mapping for any weight greater than 2 is proposed. The code construction is independent of mapping technique. It maintains crosscorrelation value of atmost $1\left(\lambda_{c} \leq 1\right)$ between all the N users. A single code construction algorithm is designed for all weights greater than 2. For each additional user, code length increment is constant. For example, if code length for 3 users is 9 then for 4 users it is 12 , for 5 users it is 15 and so on (increment of 3 for each user).

### 3.2 Code Construction

The section is divided into 2 subsections. 3.2.1 explains the code construction algorithm. 3.2.2 contains the code construction example.

### 3.2.1 Algorithm

The value of weight $(W)$ and number of users $(N)$ are chosen. Code length is given as $L=N(W-1)$ for $W$ and $N$.

Basic Matrix $(M)$ of size $2 \times(W-1)$ is constructed as follows.

$$
M=\left[\begin{array}{l}
R_{1}  \tag{3.1}\\
R_{2}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{W-2}{2}\right\rfloor 0 s & \left\lfloor\frac{W+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{W}{2}\right\rfloor 1 s & \left\lfloor\frac{W-1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times(W-1)}
$$

The complete code set is represented by matrix $U$ of size $N \times L$ for $N$ users. The construction of $U$ involves 3 steps in which an intermediary matrix $U^{*}$
is first constructed. $M$ is repeated $N-1$ times in $U^{*}$ as shown below.

$$
U^{*}=\left[\begin{array}{cccccc}
R_{1} & . . & . . & . . & . . & . .  \tag{3.2}\\
R_{2} & R_{1} & . . & . . & . . & \vdots \\
\vdots & R_{2} & R_{1} & . . & . . & \vdots \\
\vdots & \vdots & \vdots & \ddots & \ddots & \vdots \\
\vdots & \vdots & \vdots & \ddots & R_{1} & \vdots \\
. . & . . & . . & . . & R_{2} & . .
\end{array}\right]
$$

To completely fill all columns, basic matrix rows $R_{1}$ and $R_{2}$ are added to last row and first row of last column of matrix $U^{*}$ respectively as shown below.

$$
U^{* *}=\left[\begin{array}{ccccccc}
R_{1} & . . & . . & . . & . . & & R_{2}  \tag{3.3}\\
R_{2} & R_{1} & . . & . . & . . & . . & \vdots \\
\vdots & R_{2} & \ddots & \ddots & \ddots & \ddots & \vdots \\
\vdots & \vdots & \ddots & \ddots & \ddots & \ddots & \vdots \\
\vdots & \vdots & \ddots & \ddots & \ddots & R_{1} & \vdots \\
. . & . . & . . & . . & . . & R_{2} & R_{1}
\end{array}\right]_{N \times L}
$$

The complete code set is obtained by filling up empty places in $U^{* *}$ with zeros.

$$
U=\left[\begin{array}{ccccccc}
R_{1} & 0 & 0 & . . & . . & . . & R_{2}  \tag{3.4}\\
R_{2} & R_{1} & 0 & . . & . . & . . & 0 \\
0 & R_{2} & 0 & . . & . . & . . & \vdots \\
\vdots & \vdots & \vdots & \ddots & \ddots & \ddots & \vdots \\
\vdots & \vdots & \vdots & \ddots & \ddots & R_{1} & 0 \\
0 & 0 & 0 & . . & . . & R_{2} & R_{1}
\end{array}\right]_{N \times L}
$$

Algorithm is stated as:

- Choose $W, N$ and calculate the code length $L$.
- Construct $M$ as per Eq. (3.1).
- Repeat $M$ in $U^{*}$ as per Eq. (3.2).
- $R_{1}$ and $R_{2}$ are added to $U^{* *}$ as per Eq. (3.3) and empty places in $U^{* *}$ are filled with zeros to complete code construction for all users.


### 3.2.2 Code construction example

## Weight ( $W=3$ )

1. Let number of users are $N=3$. Code length is calculated as $L=$ $N(W-1)=3(2)=6$.
2. Size of matrix is defined as $2 \times(3-1)=2 \times 2$. Matrix is created as

$$
M=\left[\begin{array}{c}
R_{1} \\
R_{2}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{3-2}{2}\right\rfloor 0 s & \left\lfloor\frac{3+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{3}{2}\right\rfloor 1 s & \left\lfloor\frac{3-1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times 2}=\left[\begin{array}{ll}
1 & 1 \\
1 & 0
\end{array}\right]_{2 \times 2}
$$

3. $M$ is repeated 2 times as

$$
U^{*}=\left[\begin{array}{cccccc}
1 & 1 & . . & . . & . . & . . \\
1 & 0 & 1 & 1 & . . & . . \\
. . & . . & 1 & 0 & . . & . .
\end{array}\right]_{N \times L} .
$$

4. Matrix upper row $R_{1}$ and lower row $R_{2}$ is put in last and first row of last column respectively as

$$
U^{* *}=\left[\begin{array}{cccccc}
1 & 1 & . . & . & 1 & 0 \\
1 & 0 & 1 & 1 & . . & . . \\
. . & . . & 1 & 0 & 1 & 1 .
\end{array}\right]_{3 \times 6}
$$

CHAPTER 3. GENERALIZED CODE


Figure 3.1: SAC-OCDMA system setup for $W=3$ using Balanced Detection for generalized code.

Remaining places are filled with zeros.

$$
U=\left[\begin{array}{llllll}
1 & 1 & 0 & 0 & 1 & 0 \\
1 & 0 & 1 & 1 & 0 & 0 \\
0 & 0 & 1 & 0 & 1 & 1
\end{array}\right]_{3 \times 6}
$$

### 3.3 SAC-OCDMA system

The implementation of SAC-OCDMA system using balanced detection technique for $W=3$ using generalized code is shown in Fig.3.1. At the encoder for each user, the code is generated by selecting the wavelengths from optical signal of the broadband source. The wavelengths are selected according to the code to be transmitted over the channel. These signals are modulated
by MZM according to given data. Codes from different users are combined by using mod-2 sum before they are launched onto the optical fiber.

At receiver, the received signal divides into two arms. The upper arm of decoder uses the same wavelength structure as that of the encoder. In the lower arm of decoder, wavelength structure is given according to binary sum of columns of matrix U .

For an example of weight, $W=3$, and number of users, $N=3, U$ matrix is given as

| Wavelengths |
| :---: |
| user 1 |
| user 2 |
| user 3 |
| -- |
| Sum |\(\quad\left[\begin{array}{cccccc}\lambda_{0} \& \lambda_{1} \& \lambda_{2} \& \lambda_{3} \& \lambda_{4} \& \lambda_{5} <br>

1 \& 1 \& 0 \& 0 \& 1 \& 0 <br>
1 \& 0 \& 1 \& 1 \& 0 \& 0 <br>
0 \& 0 \& 1 \& 0 \& 1 \& 1 <br>
-- \& -- \& -- \& -- \& -- \& -- <br>
0 \& 1 \& 0 \& 1 \& 0 \& 1\end{array}\right]\).

The binary sum of all columns of matrix U gives $W-2$ non-overlapping wavelengths for each user. The non-overlapping wavelengths which are not present in desired user are used to eliminate the MAI at lower arm of decoder.

Photodiodes are used to detect the filtered optical signal. An electrical subtractor between the two arms is used to cancel out the MAI.

### 3.4 Balanced Detection Technique

Let $C_{k}(j)$ be the $j$ th element of the $k$ th proposed code sequence. At balanced receiver, the proposed code exhibits different code properties in the upper and lower arms of detector depending on particular detection technique.

In case of upper arm, detector has same structure as an encoder. The
autocorrelation function of a desired user gives a high peak of $W$. Cross correlation of interfering users with desired user is atmost 1. Correlation function for upper arm is explained as

$$
\sum_{j=1}^{L} C_{k}(j) \cdot C_{l}(j)=\left\{\begin{array}{ccc}
W & k=l & \text { same user }  \tag{3.6}\\
1 & k \neq l & l=k \pm 1 \\
0 & k \neq l & \text { other users }
\end{array}\right.
$$

In case of lower arm, the $W-2$ non-overlapping wavelengths are denoted by $C_{Z}(j)$ as shown in Section 3.3. The method to reject the MAI from interfering users is explained below. The product of $C_{Z}(j)$ and codes of interfering users ( $l=k \pm 1$ ) is considered first as

$$
\begin{equation*}
C_{X}(j)=\sum_{j=1}^{L}\left(C_{Z}(j) \cdot C_{l}(j)\right) \tag{3.7}
\end{equation*}
$$

Correlation function for lower arm is given as

$$
\begin{gather*}
\sum_{j=1}^{L} C_{k}(j) \cdot C_{X}(j)=\left\{\begin{array}{ccc}
0 & k=l & \text { same user } \\
(W-2) & k \neq l & l=k \pm 1 \text { interfering users } \\
0 & k \neq l & \text { other users }
\end{array}\right.  \tag{3.8}\\
\frac{\sum_{j=1}^{L} C_{k}(j) \cdot C_{X}(j)}{(W-2)}=\left\{\begin{array}{ccc}
0 & k=l & \text { same user } \\
1 & k \neq l & l=k \pm 1 \\
0 & k \neq l & \text { other users }
\end{array}\right. \tag{3.9}
\end{gather*}
$$

An electrical subtractor between the two arms is used to cancel out the MAI

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as

$$
\sum_{j=1}^{L} C_{k}(j) \cdot C_{l}(j)-\frac{\sum_{j=1}^{L} C_{k}(j) \cdot C_{X}(j)}{(W-2)}=\left\{\begin{array}{ccc}
W & k=l & \text { same user }  \tag{3.10}\\
0 & k \neq l & l=k \pm 1 \\
0 & k \neq l & \text { other users }
\end{array}\right.
$$

To analyse $B E R$, the Gaussian approximation with assumptions are taken as per given in Section 2.3.1. The coherence time of a thermal source [18] is given in Eq. (2.9). The variance of photocurrent [24] can be written as given in Eq. (2.10). The PSD of the received signals is written as given in Eq. (2.14). The total power incident at the input of photodetector, $P D_{1}$ of $k$ th receiver during one bit period can be written as

$$
\begin{gather*}
P\left(P D_{1}\right)=\int_{0}^{\infty} G_{1}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{l}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v \\
=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{l}(j) \tag{3.11}
\end{gather*}
$$

Using upper arm property of correlation function given in Eq. (3.6), Eq. (3.11) simplifies to

$$
\begin{equation*}
P\left(P D_{1}\right)=\frac{P_{s r} W}{L}+\frac{P_{s r}}{L} \sum_{k=1, k \neq l}^{N} d_{k} . \tag{3.12}
\end{equation*}
$$

The total power incident at the input of photodetector, $P D_{2}$ of $k$ th receiver during one bit period can be written as

$$
P\left(P D_{2}\right)=\int_{0}^{\infty} G_{2}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{X}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v
$$

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$$
\begin{equation*}
P\left(P D_{2}\right)=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{X}(j) \tag{3.13}
\end{equation*}
$$

Using lower arm property of correlation function given in Eq. (3.9), Eq. (3.13) simplifies to

$$
\begin{equation*}
P\left(P D_{2}\right)=\frac{P_{s r}}{L} \sum_{k=1, k \neq l}^{N} d_{k} \tag{3.14}
\end{equation*}
$$

The received signal of specific user is given by the difference between photocurrents $I_{1}$ and $I_{2}$, which is expressed as $I=I_{1}-I_{2} . I_{1}$ and $I_{2}$ are currents at photodiodes of upper and lower branch respectively.

$$
\begin{equation*}
I=\mathcal{R} P\left(P D_{1}\right)-\mathcal{R} P\left(P D_{2}\right) \tag{3.15}
\end{equation*}
$$

Substituting the expressions of $P\left(P D_{1}\right)$ and $P\left(P D_{2}\right)$ of total power incident at input of $P D_{1}$ and $P D_{2}$ from Eqs. (3.12) and (3.14) into Eq. (3.15), the received signal is

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r} W}{L} \tag{3.16}
\end{equation*}
$$

The shot noise power is given as

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e B\left(I_{1}+I_{2}\right)=2 e B \mathcal{R}\left[P\left(P D_{1}\right)+P\left(P D_{2}\right)\right] \tag{3.17}
\end{equation*}
$$

By substituting the values in Eq. (3.17) from Eqs. (3.12) and (3.14), shot noise is

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}(W+4)}{L} \tag{3.18}
\end{equation*}
$$

The following approximation is used as per the methodology given in [58]

$$
\begin{equation*}
\sum_{k=1}^{N} C_{k}(j) \approx \frac{N W}{L} \tag{3.19}
\end{equation*}
$$

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. The PIIN power can be written as

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=B I_{1}^{2} \tau_{c 1}+B I_{2}^{2} \tau_{c 2}=B \mathcal{R}^{2}\left[\int_{0}^{\infty} G_{1}^{2}(v) d v+\int_{0}^{\infty} G_{2}^{2}(v) d v\right] \tag{3.20}
\end{equation*}
$$

By substituting values in Eq. (3.20) from Eqs. (3.12) and (3.14), PIIN is

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2} N W}{L^{2} \Delta v}[W+4] \tag{3.21}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ as given in Eq. (2.10) is expressed as

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}(W+4)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W(W+4)}{L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}} . \tag{3.22}
\end{equation*}
$$

Noting that the probability of sending bit 1 at any time for each user is half [58], Eq. (3.22) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{P_{s r} e B \mathcal{R}(W+4)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W[W+4]}{2 L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{3.23}
\end{equation*}
$$

Substituting from Eqs. (3.16) and (3.23) in Eq. (2.29), $S N R$ is expressed as

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s r} W}{L}\right)^{2}}{\frac{e B \mathcal{R} P_{s r}(W+4)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W(W+4)}{2 L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}}} \tag{3.24}
\end{equation*}
$$

The $B E R$ using Gaussian approximation from $S N R$ is expressed as given in Eq. (2.31).

### 3.5 Direct Detection Technique

The implementation of SAC-OCDMA system using DD for $W=3$ and $N=3$ (generalized code) is shown in Fig.3.2. DD uses the non-overlapping wave-


Figure 3.2: SAC-OCDMA system setup for $W=3$ using DD for generalized code.
lengths in its detection process. Non-overlapping wavelengths are calculated by mod- 2 sum of all users as shown in Eq. (3.5). At receiver, the nonoverlapping wavelengths, which are unique for each user are selected and sent to photo diode. It requires a single photo detector for detecting the wavelengths without any subtractor as used in balanced detection (Section 3.3). PIIN is theoretically eliminated on detecting non-overlapping wavelengths. This results in reduced complexity of receiver along with performance improvement.

For BD, signal is divided into two parts which are detected and converted into electrical signal, which is followed by electrical subtractor. BD technique require more processing and more components as compare to DD. In DD, only single photodiode need to detect signal. DD requires less components which turn to reduce cost of recevier. DD requires less processing which leads to less complexity at recevier $[56,85]$.

Let $C_{k}(j)$ be the $j$ th element of the $k$ th proposed code sequence. The $W-2$ non-overlapping wavelengths for each user from $C_{Z}(j)$ is selected by product of $C_{Z}(j)$ and with desired user. Correlation function is given as

$$
C_{X}(j)=\sum_{j=1}^{L}\left(C_{Z}(j) \cdot C_{k}(j)\right)=\left\{\begin{array}{cll}
W-2 & k=l & \text { same user }  \tag{3.25}\\
0 & k \neq l & \text { other users }
\end{array} .\right.
$$

For $B E R$ analysis, the Gaussian approximation and all other assumptions are same as used in Section 2.3.1. The variance of photocurrent due to the detection of an ideally unpolarized thermal light can be written as [56, 85]:

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\left\langle I_{\text {shot }}^{2}\right\rangle+\left\langle I_{\text {thermal }}^{2}\right\rangle . \tag{3.26}
\end{equation*}
$$

here $\left\langle I_{\text {shot }}^{2}\right\rangle$, and $\left\langle I_{\text {thermal }}^{2}\right\rangle$ are Shot noise and Thermal noise respectively. The expressions of $\left\langle I_{\text {shot }}^{2}\right\rangle$, and $\left\langle I_{\text {thermal }}^{2}\right\rangle$ are as given in Eqs. (2.12),(2.13). The PSD of the received optical signal is expressed in Eq. (2.14)

After selecting non-overlapping wavelengths, total power incident at the input of photodiode of $k$ th receiver during one bit period can be given as

$$
\begin{align*}
\int_{0}^{\infty} G(v) d v= & \int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{X}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v \\
& =\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{X}(j) \tag{3.27}
\end{align*}
$$

Using correlation property given in Eq. (3.25), Eq. (3.27) can be written as

$$
\begin{equation*}
\int_{0}^{\infty} G(v) d v=\frac{P_{s r}(W-2)}{L} . \tag{3.28}
\end{equation*}
$$

The photo current generated by the incident optical power is given by

$$
\begin{equation*}
I=\mathcal{R} \int_{0}^{\infty} G(v) d v \tag{3.29}
\end{equation*}
$$

Put the value from Eq. (3.28) into Eq. (3.29) for total power incident at input of $P D$. The resultant photo current is

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r}(W-2)}{L} . \tag{3.30}
\end{equation*}
$$

By substituting the values in Eq. (2.10) from Eq. (3.30), shot noise is

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e B \mathcal{R}\left(\frac{P_{s r}(W-2)}{L}\right) \tag{3.31}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ is expressed as:

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=2 e B \mathcal{R}\left[\frac{P_{s r}(W-2)}{L}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{3.32}
\end{equation*}
$$

Noting that the probability of sending bit 1 at any time for each user is half [58], Eqs. (3.32) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=e B \mathcal{R}\left[\frac{P_{s r}(W-2)}{L}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{3.33}
\end{equation*}
$$

Substituting from Eqs. (3.30), (3.33) in Eq. (2.29), $S N R$ is expressed as

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s r}(W-2)}{L}\right)^{2}}{e B \mathcal{R}\left[\frac{P_{s r}(W-2)}{L}\right]+\frac{4 K_{b} T_{n} B}{R_{L}}} \tag{3.34}
\end{equation*}
$$

The Bit Error Rate $(B E R)$ is calculated as given in Eq. (2.31).


Figure 3.3: Comparision of MDW and EDW code with Generalized code.

### 3.6 Numerical Results

To calculate the numerical results, the relevant parameters are listed in Table 2.2.

Figure 3.3 depicts the $B E R$ versus number of users for EDW $(W=3)$, MDW $(W=4)$ and generalized code for $(W=3,4)$ at a data rate of 622 Mbps using balanced detection. At $B E R$ of $10^{-9}$, number of users are 61 and 58 for $W=3$ and $W=4$ respectively for generalized code. The number of users for EDW $(W=3)$ and MDW $(W=4)$ are 34 and 61 respectively. The variation of results are due to difference in code length which depends on the number of users and its dependency on mapping for EDW and MDW which affects the $B E R$ performance. The $B E R$ for EDW and MDW depends on the size of basic matrix. $B E R$ changes on varying the size of basic matrix which further changes the length of code on increasing number of users. The designing of code without mapping eliminates the effect of basic matrix dimensions on $B E R$.
$B E R$ is plotted against number of users when weight is varying from 3 to 6 using balanced detection for generalized code as shown in Fig.3.4. At

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$B E R$ of $10^{-9}$, number of users are $57,61,63$ and 64 for $W=3,4,5$ and 6 respectively. As the weight is increased auto correlation peak value ( $W$ ) increases which reduces the error probability. Resultant number of users for same $B E R$ is increased along with increased code length. As the weight is increased, the number of pulses per code increases which in turn increases the signal power per user. As a result $S N R$ and hence $B E R$ improves.

Figure 3.5 depicts the affect of datarate on $B E R$ at constant value of $W=4$ using balanced detection for generalized code. $B E R$ is plotted against number of users $(N)$ with increasing data rate. Number of users are 34, 19 and 10 for data rate $1.25 \mathrm{Gbps}, 2.5 \mathrm{Gbps}$ and 5 Gbps respectively at $B E R$ of $10^{-9}$. As the data rate of the system is increased, $B E R$ is increased for system which degrades the number of supportable users for same $B E R$. This happens due to increase in required bandwidth which increases the noise in system. Hence number of users are reduced on increasing data rate as shown in Figure 3.5.

Balanced detection and DD are two different detection techniques. Both are different ways to detect code for each user. Balanced detection use various techniques to select wavelengths for lower arm such as complementary technique, $A N D$ technique, and Ex-OR technique. For generalized code, binary sum technique is used for theoretical and numerical results. For DD, binary sum technique is used to select the non-overlapping wavelengths. These non-overlapping wavelengths after filtering are sent to the photodiode. The middle term of denominator of Eq. (3.24) is due to PIIN for BD. Similar expression for DD is not required as in Eq. (3.34). Further weight factor in $S N R$ expressions for BD and DD are different.
$B E R$ is plotted against number of users for balanced detection and DD using generalized code for $W=6$ as shown in Fig.3.6. Number of users are


Figure 3.4: Comparison of BER for different weights using Generalized code.


Figure 3.5: Comparison of datarate for $W=4$ using generalized code.

64 and 71 for balanced detection and DD respectively at $B E R$ of $10^{-9}$. Due to elimination of PIIN for DD, performance is improved and, the receiver complexity and cost of receiver design is reduced.



Figure 3.6: Comparison of $B E R$ for de- Figure 3.7: $B E R$ (PIIN, shot and thertection techniques $(W=6)$ using gen- mal noise) versus received power $\left(P_{s r}\right)$ eralized code. at $N=15$ and $W=4$ using balanced detection.

Figure 3.7 illustrates the $B E R$ (PIIN, Shot and thermal noise) versus received power using balanced detection for $N=15$ and $W=4$. As shown in Fig. 3.7, the main factor which degrades system performance is PIIN using balanced detection. It occurs due to fluctuations in intensity of the received
signal which results in variance of the received signal. It cannot be improved by increasing the transmitted power. PIIN also depends on the number of interfering users and increases with increasing interfering users. On the other hand, shot noise reduces with increase in received power.

### 3.7 Summary

A new generalized algorithm to construct EDW and MDW like codes without mapping for any weight greater than 2 is proposed. Code construction is independent of mapping technique. The proposed algorithm is for Constant Length (CL) and Constant Weight (CW). The code length increment is constant for each additional user. First, it constructs a basic matrix for particular weight. Secondly, it is repeated for each row upto $(N-1)$ times. Lastly, rows of basic matrix is added and all empty spaces are filled with zeros. It maintains crosscorrelation value of atmost $1\left(\lambda_{c} \leq 1\right)$ between any two of the users. The numerical results using balanced detection and direct detection are obtained and compared.

# Variable Weight Construction using Generalized code 

### 4.1 Introduction

The codes with fixed code length and weight are not suitable for multimedia services. Thus, coding techniques with variable code weights and code lengths are required. The code weight indicates the amount of power sent by each code. Higher code weight means higher transmitted power and vice versa. Variable Weight (VW) algorithm is proposed which is based on Generalized Optical Code construction for Enhanced and Modified Double Weight codes as discussed in Chapter 3. The proposed algorithm can be used for any combination of weights greater than 2 . The cross correlation between any two users is at most 1. This code construction algorithm ensures higher power at receiver for higher weight users. Lower weight users receive less power compared to higher weight users. The difference in received power
translates as varying performance, and is useful for multimedia applications.

### 4.2 Code Construction

### 4.2.1 Algorithm

The fundamental equations to find the basic matrix is based on as given in Section 3.2. The steps involved in code construction using proposed algorithm are given below

1. The cardinality or total number of users $\left(N_{\max }\right)$ is given by

$$
\begin{equation*}
N_{\max }=\sum_{i=1}^{N} N_{W_{i}} \tag{4.1}
\end{equation*}
$$

$N_{W_{i}}$ represents number of users with weight ' $W_{i}$ '. The value of $W_{i}$ must be greater than 2 .
2. For all weights, basic matrix $\left(M_{W_{i}}\right)$ of size $2 \times\left(W_{i}-1\right)$ is constructed as

$$
M_{W_{i}}=\left[\begin{array}{c}
R_{1}^{\left(W_{i}\right)}  \tag{4.2}\\
R_{2}^{\left(W_{i}\right)}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{W_{i}-2}{2}\right\rfloor 0 s & \left\lfloor\frac{W_{i}+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{W_{i}}{2}\right\rfloor 1 s & \left\lfloor\frac{W_{i}-1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times\left(W_{i}-1\right)}
$$

$W_{i}$ is any of the weights from $W_{1}$ to $W_{N}$.
3. Code construction starts from highest weight $\left(W_{N}\right)$ and ends with lowest weight $\left(W_{1}\right)$.
4. Basic matrix of highest weight $\left(W_{N}\right)$ is repeated $\left(N_{W_{N}}+1\right)$ times as

$$
U=\left[\begin{array}{ccccc}
R_{1}^{\left(W_{N}\right)} & . . & . . & . . & . .  \tag{4.3}\\
R_{2}^{\left(W_{N}\right)} & R_{1}^{\left(W_{N}\right)} & . . & . . & . . \\
. . & R_{2}^{\left(W_{N}\right)} & R_{1}^{\left(W_{N}\right)} & . . & . . \\
. . & . . & \ddots & . . & . . \\
. . & . . & \ddots & R_{2}^{\left(W_{N}\right)} & R_{1}^{\left(W_{N}\right)} \\
\vdots & \vdots & \vdots & \vdots & R_{2}^{\left(W_{N}\right)}
\end{array}\right] .
$$

5. For last repeated basic matrix of $W_{N}$, calculate reducibility number $\left(S_{W_{N}}\right)$.
(a) Reducibility number $\left(S_{W_{i}}\right)$ is defined as

$$
\begin{equation*}
S_{W_{i}}=\left\lfloor\frac{W_{i}}{2}\right\rfloor-\left\lfloor\frac{W_{i-1}}{2}\right\rfloor \tag{4.4}
\end{equation*}
$$

i. Calculated value of $S_{W_{i}}$ is either 0 or any integer value.
ii. When $S_{W_{i}}=0$, no change is required in basic matrix $M_{W_{i}}$.
iii. When $S_{W_{i}}=$ integer, reduce $S_{W_{i}}$ number of columns from left of last repeated $M_{W_{i}}$.
iv. After reduction, last repeated basic matrix is updated as $\left(R_{1 S}^{\left(W_{N}\right)}, R_{2 S}^{\left(W_{N}\right)}\right)$.

$$
U=\left[\begin{array}{ccccc}
R_{1}^{\left(W_{N}\right)} . . & . . & & &  \tag{4.5}\\
R_{2}^{\left(W_{N}\right)} . . & R_{1 S}^{\left(W_{N}\right)} & & & \\
\ldots . & R_{2 S}^{\left(W_{N}\right)} & R_{1}^{\left(W_{N-1}\right)} . . & . . & \\
\vdots & \vdots & R_{2}^{\left(W_{N-1}\right)} . . & R_{1 S}^{\left(W_{N-1}\right)} & \\
\vdots & \vdots & \vdots & R_{2 S}^{\left(W_{N-1}\right)} & . .
\end{array}\right] .
$$

6. Steps 4 and 5 are repeated for weights $W_{N-2}$ to $W_{1}$. Basic matrix of
$W_{N-2}$ to $W_{1}$ are repeated $N_{W_{N-2}}$ to $N_{W_{1}}$ times respectively as given in Eq. (6.8).

$$
U=\left[\begin{array}{cccccccc}
R_{1}^{\left(W_{N}\right)} \ldots . . & & & & & & &  \tag{4.6}\\
R_{2}^{\left(W_{N}\right)} . . & R_{1 S}^{\left(W_{N}\right)} & & & & & & \\
\ldots . & R_{2 S}^{\left(W_{N}\right)} & R_{1}^{\left(W_{(N-1)}\right)} . . & & & & & \\
\vdots & \vdots & R_{2}^{\left(W_{(N-1)}\right)} . . & R_{1 S}^{\left(W_{(N-1)}\right)} & & & & \\
\vdots & \vdots & \vdots & \ddots & & & & \\
\vdots & \vdots & \vdots & \ddots & R_{1 S}^{\left(W_{2}\right)} & & & \\
\vdots & \vdots & \vdots & \vdots & R_{2 S}^{\left(W_{2}\right)} & R_{1}^{\left(W_{1}\right)} & & \\
\vdots & \vdots & \vdots & \vdots & \vdots & R_{2}^{\left(W_{1}\right)} & & \\
\vdots & \vdots & \vdots & \vdots & \vdots & \ddots & & \\
. . & . . & \ldots & . . & . . & . . & R_{2}^{\left(W_{1}\right)} & R_{1}^{\left(W_{1}\right)} \\
\ldots & . . & . . & . . & . . & . . & . . & R_{2}^{\left(W_{1}\right)}
\end{array}\right]
$$

7. First and last rows of $U$ matrix are removed as shown in Eq. (4.7).

$$
U=\left[\begin{array}{cccccccc}
R_{2 S}^{\left(W_{N}\right)} & . . & R_{1 S}^{\left(W_{N}\right)} & & & & &  \tag{4.7}\\
. . & . . & R_{2 S}^{\left(W_{N}\right)} & R_{1}^{\left(W_{(N-1)}\right)} & & & & \\
\vdots & \vdots & \vdots & R_{2}^{\left(W_{(N-1)}\right)} & & & & \\
\vdots & \vdots & \vdots & \vdots & \vdots & \ddots & & \\
\vdots & \vdots & \vdots & \vdots & \ddots & \ddots & R_{1}^{W_{1}} & \\
. . & . . & . . & . . & . . & . . & R_{2}^{W_{1}} & R_{1}^{W_{1}}
\end{array}\right]
$$

8. All empty spaces are filled with zeros.
9. Because of Step 7, all columns filled with zeros are deleted from $U$ matrix. $\left(\left\lfloor\frac{W_{N}}{2}\right\rfloor+1\right)^{\text {th }}$ column to $\left(\left\lfloor\frac{W_{N}}{2}\right\rfloor+\left\lfloor\frac{W_{N}-1}{2}\right\rfloor\right)^{\text {th }}$ columns from left side, and $\left(\left\lfloor\frac{W_{1}+1}{2}\right\rfloor+1\right)^{\text {th }}$ column to $\left(\left\lfloor\frac{W_{1}+1}{2}\right\rfloor+\left\lfloor\frac{W_{1}-2}{2}\right\rfloor\right)^{\text {th }}$ from right
side would be zeros, when $W_{1}$ is greater than 3 . If $W_{1}$ is equal to 3 , there are no columns of zeros from right side.

The complete code set is generated after step 9. The total code length $\left(L_{T}\right)$ is the number of wavelengths required by the system for all weights. The total code length is the sum of code lengths ' $L_{W_{i}}$ ' corresponding to weights ' $W_{i}$ '. Code length calculation for different weights is explained below For $N_{W_{N}}$ users,

$$
\begin{equation*}
L_{W_{N}}=\left(W_{N}-1\right) *\left(N_{W_{N}}+1\right)-S_{W_{N}}-\left\lfloor\frac{W_{N}-1}{2}\right\rfloor . \tag{4.8}
\end{equation*}
$$

For $N_{W_{N-1}}$ users

$$
\begin{equation*}
L_{W_{N-1}}=\left(W_{N-1}-1\right) *\left(N_{W_{N-1}}\right)-S_{W_{N-1}} . \tag{4.9}
\end{equation*}
$$

Similarly, lengths $L_{W_{N-2}}$ to $L_{W_{1}}$ for corresponding weights $W_{N-2}$ to $W_{1}$ are found as follows. For $N_{W_{N-2}}$ users

$$
\begin{equation*}
L_{W_{N-2}}=\left(W_{N-2}-1\right) *\left(N_{W_{N-2}}\right)-S_{W_{N-2}} . \tag{4.10}
\end{equation*}
$$

For $N_{W_{1}}$ users

$$
\begin{equation*}
L_{W_{1}}=\left(W_{1}-1\right) *\left(N_{W_{1}}\right)-\left\lfloor\frac{W_{1}-2}{2}\right\rfloor . \tag{4.11}
\end{equation*}
$$

Total code length $\left(L_{T}\right)$ used by the VW code is given as

$$
\begin{equation*}
L_{T}=L_{W_{N}}+L_{W_{N-1}}+\cdots+L_{W_{1}} . \tag{4.12}
\end{equation*}
$$

Flow chart of the algorithm indicating code construction steps is shown in Fig. 4.1. The comparison of code properties of proposed code with KS and RD codes is given in Table 4.1.


Figure 4.1: Code construction flow chart for proposed VW code.

### 4.2.2 Code Construction Example

Number of users $\left(N_{2}\right)$ and $\left(N_{1}\right)$ are chosen as 3 each for higher weight ( $W_{2}=$
$4)$ and lower weight $\left(W_{1}=3\right)$.

1. Size of basic matrix for weight $W_{2}=4$ is $2 \times(4-1)=2 \times 3$, and is created as

$$
M_{W_{2}}=\left[\begin{array}{l}
R_{1}^{(4)} \\
R_{2}^{(4)}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{4-2}{2}\right\rfloor 0 s & \left\lfloor\frac{4+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{4}{2}\right\rfloor 1 s & \left\lfloor\frac{4-1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times 3}=\left[\begin{array}{lll}
0 & 1 & 1 \\
1 & 1 & 0
\end{array}\right]_{2 \times 3}
$$

2. Size of basic matrix for weight $W_{1}=3$ is $2 \times(3-1)=2 \times 2$, and is created as

$$
M_{W_{1}}=\left[\begin{array}{l}
R_{1}^{(3)} \\
R_{2}^{(3)}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{3-2}{2}\right\rfloor 0 s & \left\lfloor\frac{3+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{3}{2}\right\rfloor 1 s & \left\lfloor\frac{3-1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times 2}=\left[\begin{array}{ll}
1 & 1 \\
1 & 0
\end{array}\right]_{2 \times 2}
$$

3. $M_{W_{2}}$ is repeated $N_{2}+1=4$ times to get

$$
U=\left[\begin{array}{cccc}
011 & . . & . . & . . \\
110 & 011 & . . & . . \\
. . & 110 & 011 & . . \\
. . & . . & 110 & (0) 11 \\
. . & . . & . . & (1) 10
\end{array}\right]
$$

4. Find $S_{W_{2}}=2-1=1$. Reduce a single 1 from $R_{2}^{(4)}$, and a single 0 from $R_{1}^{(4)}$ from basic matrix $M_{W_{2}}$ as shown in steps 3 and 4 of Section 4.2.1. The 1's and 0's reduced in step 4 are indicated in parenthesis in step 3.

$$
U=\left[\begin{array}{cccc}
011 & . . & . . & . . \\
110 & 011 & . . & . . \\
. . & 110 & 011 & . . \\
. . & . . & 110 & 11 \\
. . & . . & . . & 10
\end{array}\right] .
$$

5. $M_{W_{1}}$ is repeated $N_{1}=3$ times as

$$
U=\left[\begin{array}{ccccccc}
011 & . . & . . & . . & & & \\
110 & 011 & . . & . . & & & \\
. . & 110 & 011 & . . & & & \\
. . & . . & 110 & 11 & & & \\
. . & . . & . . & 10 & 11 & . . & . . \\
. . & . . & . . & . . & 10 & 11 & . . \\
. . & . . & . . & . . & . . & 10 & 11 \\
. . & . . & . . & . . & . . & . . & 10
\end{array}\right] .
$$

6. First and last rows of $U$ matrix are removed to get

$$
U=\left[\begin{array}{ccccccc}
110 & 011 & . . & . . & & & \\
. . & 110 & 011 & . . & & & \\
. . & . . & 110 & 11 & & & \\
. . & . . & . . & 10 & 11 & . . & . . \\
. . & . . & . . & . . & 10 & 11 & . . \\
. . & . . & . . & . . & . . & 10 & 11
\end{array}\right] .
$$

7. All empty spaces are filled with zeros, and all empty columns are deleted indicated by parenthesis.

$$
U=\left[\begin{array}{lllllll}
11(0) & 011 & 000 & 00 & 00 & 00 & 00 \\
00(0) & 110 & 011 & 00 & 00 & 00 & 00 \\
00(0) & 000 & 110 & 11 & 00 & 00 & 00 \\
00(0) & 000 & 000 & 10 & 11 & 00 & 00 \\
00(0) & 000 & 000 & 00 & 10 & 11 & 00 \\
00(0) & 000 & 000 & 00 & 00 & 10 & 11
\end{array}\right]
$$

8. Code is generated for 6 users using two different weights.

$$
\begin{gather*}
C_{1}  \tag{4.13}\\
C_{2} \\
C_{3} \\
C_{4} \\
C_{5} \\
C_{6} \\
\text { BinarySum }
\end{gather*} \quad\left[\begin{array}{ccccccc}
11 & 011 & 000 & 00 & 00 & 00 & 00 \\
00 & 110 & 011 & 00 & 00 & 00 & 00 \\
00 & 000 & 110 & 11 & 00 & 00 & 00 \\
00 & 000 & 000 & 10 & 11 & 00 & 00 \\
00 & 000 & 000 & 00 & 10 & 11 & 00 \\
00 & 000 & 000 & 00 & 00 & 10 & 11 \\
& 101 & 101 & 01 & 01 & 01 & 11
\end{array}\right] .
$$

9. Code length for higher weight is $L_{W_{2}}=(4-1) *(3+1)-1-1=10$, and for lower weight is $L_{W_{1}}=(3-1) *(3)=6$. The total code length $L_{T}$ for code is $L_{W_{2}}+L_{W_{1}}=16$.

In the example, we can see that some of the 1's are clubbed together. With increase in weight, more number of 1's would be clubbed together. Hence, for realisation of system, only filter linewidth needs to be changed with respect to number of 1's clubbed together.

### 4.3 Bit Error Rate calculation

The Gaussian approximation is considered to determine $B E R$ along mathematical analysis as given in Section 2.3.1. Coherence time is defined as given in Eq. (2.9). The noise variance of photocurrent as a result of an ideally unpolarized thermal light detection, which is produced due to spontaneous emission, can be given in Eq. (2.10)

Let $C_{h}(j)$ be the $j$ th element of the $h$ th proposed code. At receiver, PSD is given as

$$
\begin{equation*}
r(v)=\frac{P_{s r}}{\Delta v} \sum_{h=1}^{N_{\max }} d_{h} \sum_{j=1}^{L_{T}} C_{h}(j) r e c(j) \tag{4.14}
\end{equation*}
$$

Here effective power of a broadband source $P_{s r}$ is received at receiver, the data bit of $h$ th user is denoted by $d_{h}$ and the function $\operatorname{rec}(i)$ in Eq.(4.14) is given in Eq. (2.15)

### 4.3.1 Balanced Detection Technique

BD technique is described in Sections 2.3.1, 3.3 and 3.4. Upper arm, correlation function is given as

$$
\sum_{j=1}^{L_{T}} C_{h}(j) \cdot C_{f}(j)=\left\{\begin{array}{ccc}
W_{i} & h=f & \text { same user }  \tag{4.15}\\
1 & h \neq f & f=h \pm 1 \\
0 & h \neq f & \text { other users }
\end{array}\right.
$$

For desired user, all wavelengths are detected by upper arm. To reduce the effect of MAI from undesired user's wavelengths at upper arm, lower arm is used. Correlation function of lower arm is formed by following the steps outlined below.

1. The binary sum of all non-overlapping wavelengths $\left(C_{Y}(j)\right)$ for all users is determined as shown in Eq. 4.13.
2. The binary sum of all columns of generated code matrix gives $W_{i}-2$ non-overlapping wavelengths. The non-overlapping wavelengths which are not present in desired user are used to eliminate the MAI at lower arm of decoder.
3. The product of $C_{Y}(j)$ with interfering users code is given as

$$
\begin{equation*}
C_{Z}(j)=\sum_{j=1}^{L_{T}}\left(C_{Y}(j) \cdot C_{f}(j)\right) \tag{4.16}
\end{equation*}
$$

Considering desired user as $C_{3}$ and interfering users as $C_{2}$ and $C_{4}$ from Eq. 4.13. $C_{Y}(j)$ is the last row of Eq. 4.13. For $C_{f}(j)=$ $C_{2}(j) ; C_{Z 2}(j)=[0010000100000000]$. For $C_{f}(j)=C_{4}(j) ; C_{Z 4}(j)=$ [0000000000010000].
4. At lower arm, correlation function is written as

$$
C F=\sum_{j=1}^{L_{T}} C_{h}(j) \cdot C_{Z}(j)=\left\{\begin{array}{ccl}
0 & h=f & \text { same user }  \tag{4.17}\\
\left(W_{i}-2\right) & h \neq f & f=h \pm 1 \\
0 & h \neq f & \text { other users }
\end{array}\right.
$$

Any one of the ( $W_{i}-2$ ) wavelengths from an interfering users' $C_{Z}$ can be used in the lower arm.

To reduce MAI due to user2; $C F_{2}=C_{3} \cdot C_{Z 2}=[0000000100000000]$.
Similarly, for user4; $C F_{4}=C_{3} . C_{Z 4}=[0000000000010000]$.

Signals from upper arm and lower arm are sent to an electrical subtractor to cancel out the MAI. The correlation function changes to

$$
C F^{\prime}=\left\{\begin{array}{ccc}
W_{i} & h=f & \text { same user }  \tag{4.18}\\
0 & h \neq f & f=h \pm 1 \\
0 & h \neq f & \text { other users }
\end{array}\right.
$$

At photodetector $\left(P D_{U}\right)$ of $h$ th receiver, total power incident for one bit period is given below

$$
\begin{gather*}
P\left(P D_{U}\right)=\int_{0}^{\infty} G_{1}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{h=1}^{N_{\max }} d_{h} \sum_{j=1}^{L_{T}} C_{h}(j) C_{f}(j) \operatorname{rect}(j)\right] d v . \\
=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L_{T}} \sum_{h=1}^{N_{\max }} d_{h} \sum_{j=1}^{L_{T}} C_{h}(j) C_{f}(j) \tag{4.19}
\end{gather*}
$$

Eq. (4.19) is reduced by using correlation property of upper arm as given in Eq. (4.15), and it is written as

$$
\begin{equation*}
P\left(P D_{U}\right)=\frac{P_{s r} W_{i}}{L_{T}}+\frac{P_{s r}}{L_{T}} \sum_{h=1, h \neq f}^{N_{\max }} d_{h} . \tag{4.20}
\end{equation*}
$$

At photodetector $\left(P D_{L}\right)$ of $h$ th receiver, total power incident for one bit period is given below

$$
P\left(P D_{L}\right)=\int_{0}^{\infty} G_{2}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{h=1}^{N_{\max }} d_{h} \sum_{j=1}^{L_{T}} C_{h}(j) C_{Z}(j) r e c t(j)\right] d v
$$

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$$
\begin{equation*}
P\left(P D_{L}\right)=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L_{T}} \sum_{h=1}^{N_{\max }} d_{h} C F \tag{4.21}
\end{equation*}
$$

Eq. (4.21) is reduced by using correlation property of lower arm as given in Eq. (4.18), and it is written as

$$
\begin{equation*}
P\left(P D_{L}\right)=\frac{P_{s r}}{L_{T}} \sum_{h=1, h \neq f}^{N_{\max }} d_{h} \tag{4.22}
\end{equation*}
$$

The received signal of desired user is obtained by subtracting the lower arm photocurrent $\left(I_{L}\right)$ from upper arm photocurrent $\left(I_{U}\right)$, which is expressed as $I=I_{U}-I_{L}$.

$$
\begin{equation*}
I=\mathcal{R} P\left(P D_{U}\right)-\mathcal{R} P\left(P D_{L}\right) \tag{4.23}
\end{equation*}
$$

Here $\mathcal{R}=\eta e /\left(h \nu_{0}\right)$ is the responsivity, and $\eta$ is the internal quantum efficiency of photodiode, $\left(h \nu_{0}\right)$ is the photon energy, and $h$ is Planck's constant.

Substituting $P\left(P D_{U}\right)$ and $P\left(P D_{L}\right)$ from Eqs. (4.20) and (4.22) into Eq. (4.23), the received signal leads to

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r} W_{i}}{L_{T}} \tag{4.24}
\end{equation*}
$$

The power of shot noise is found as

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e B\left(I_{U}+I_{L}\right)=2 e B \mathcal{R}\left[P\left(P D_{U}\right)+P\left(P D_{L}\right)\right] \tag{4.25}
\end{equation*}
$$

On putting the values from Eqs. (4.20) and (4.22) in Eq. (4.25), shot noise leads to

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}\left(W_{i}+4\right)}{L_{T}} \tag{4.26}
\end{equation*}
$$

The total number of users at a given time is the summation of users with different weights that coexist in a single system [42], denoted by

$$
\begin{equation*}
\sum_{h=1}^{N_{\max }} C_{h}=\frac{1}{L_{T}} \sum_{i=1}^{N} N_{W_{i}} W_{i} . \tag{4.27}
\end{equation*}
$$

The power of PIIN is given as

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=B I_{U}^{2} \tau_{c 1}+B I_{L}^{2} \tau_{c 2}=B \mathcal{R}^{2}\left[\int_{0}^{\infty} G_{1}^{2}(v) d v+\int_{0}^{\infty} G_{2}^{2}(v) d v\right] \tag{4.28}
\end{equation*}
$$

Substituting the expressions from Eqs. (4.20), (4.22) and (4.27) in Eq. (4.28), PIIN leads to

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s s}^{2}}{L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\max }} N_{W_{i}} W_{i}\left[W_{i}+4\right] \tag{4.29}
\end{equation*}
$$

Substituting the expressions from Eqs. (4.26) and (4.29) in Eq. (2.10), the noise power is expressed as

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}\left(W_{i}+4\right)}{L_{T}}+\frac{B \mathcal{R}^{2} P_{s r}^{2}}{L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\max }} N_{W_{i}} W_{i}\left[W_{i}+4\right]+\frac{4 K_{b} T_{n} B}{R_{L}} . \tag{4.30}
\end{equation*}
$$

Since the probability for transmitting a bit 1 is half, Eq. (4.30) turns to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{P_{s r} e B \mathcal{R}\left(W_{i}+4\right)}{L_{T}}+\frac{B \mathcal{R}^{2} P_{s r}^{2}}{2 L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\max }} N_{W_{i}} W_{i}\left[W_{i}+4\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{4.31}
\end{equation*}
$$

The Signal to Noise Ratio ( $S N R$ ) is defined in Eq. (2.29). The values from Eqs. (4.24) and (4.31) are put in Eq. (2.29), $S N R$ is given as

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s s} W_{i}}{L_{T}}\right)^{2}}{\frac{P_{s r e} e B \mathcal{R}\left(W_{i}+4\right)}{L_{T}}+\frac{B \mathcal{R}^{2} P_{s r}^{2}}{L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\max }} N_{W_{i}} W_{i}\left[W_{i}+4\right]+\frac{4 K_{b} T_{n} B}{R_{L}}} . \tag{4.32}
\end{equation*}
$$

The $B E R$ is calculated as given in Eq. (2.31).

### 4.3.2 Direct Detection Technique

In DD , the $\left(W_{i}-2\right)$ non-overlapping wavelengths $\left(C_{Y}(j)\right)$ are incident on photodetector. Correlation function is written as

$$
C_{Z}(j)=\sum_{j=1}^{L_{T}}\left(C_{Y}(j) \cdot C_{h}(j)\right)=\left\{\begin{array}{cll}
W_{i}-2 & h=f & \text { same user }  \tag{4.33}\\
0 & h \neq f & \text { other users }
\end{array}\right.
$$

To analysze $B E R$, all the assumptions including Gaussian approximation are similar to that described in Sections 3.4 and 3.5. The variance of photocurrent can be given as [43]

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\left\langle I_{\text {shot }}^{2}\right\rangle+\left\langle I_{\text {thermal }}^{2}\right\rangle \tag{4.34}
\end{equation*}
$$

Non-overlapped wavelengths are filtered and sent to the photodiode of $h$ th receiver. For one bit duration, total power at $h$ th receiver is calculated as

$$
\begin{align*}
\int_{0}^{\infty} G(v) d v= & \int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{h=1}^{N_{\max }} d_{h} \sum_{j=1}^{L_{T}} C_{h}(j) C_{Z}(j) r e c(j)\right] d v  \tag{4.35}\\
& =\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L_{T}} \sum_{h=1}^{N_{\max }} d_{h} \sum_{j=1}^{L_{T}} C_{c}(j) C_{Z}(j) \tag{4.36}
\end{align*}
$$

Eq. (4.36) is rewritten in Eq. (4.37) after applying the correlation property from Eq. (4.33) as

$$
\begin{equation*}
\int_{0}^{\infty} G(v) d v=\frac{P_{s r}\left(W_{i}-2\right)}{L_{T}} . \tag{4.37}
\end{equation*}
$$

Substituting Eq. (4.37) in Eq. (3.29), photocurrent simplifies to

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r}\left(W_{i}-2\right)}{L_{T}} \tag{4.38}
\end{equation*}
$$

From Eq. (4.38), shot noise is calculated by putting the value of $I$ in Eq.

Table 4.1: Comparison of properties between different VW codes expressions.

| Code | Variable weights | Code Length | $\lambda_{c}$ | Mapping |
| :---: | :---: | :---: | :---: | :---: |
| Proposed | $W_{1}$ to $W_{N}$ | $L_{T}$ (Eq. 12) | $\leq 1$ | not used |
| VW RD | $W_{1}$ to $W_{N}$ | $L_{i}=N_{i}+2 W_{i}-3, L_{T}=\sum_{1}^{W_{N}} L_{i}$ | $\geq 1$ | used |
|  |  | $L_{T}=\sum_{1}^{W_{N}} L_{i}$ |  |  |
| VW KS | $W_{1}$ to $W_{N}$ | $L_{i}=3\left\lceil\left(\frac{N_{i}}{\left(W_{i} / 2\right)+1}\right)\right\rceil \sum_{1}^{W_{i} / 2} j, L_{T}=\sum_{1}^{W_{N}} L_{i} \leq 1$ | used |  |
|  |  | $L_{T}=\sum_{1}^{W_{N}} L_{i}$ |  |  |

(2.12) as

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e B \mathcal{R}\left(\frac{P_{s r}\left(W_{i}-2\right)}{L_{T}}\right) \tag{4.39}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ is given as:

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=2 e B \mathcal{R}\left[\frac{P_{s r}\left(W_{i}-2\right)}{L_{T}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{4.40}
\end{equation*}
$$

Since the probability of transmitting 1 for any user is half, Eq. (4.40) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=e B \mathcal{R}\left[\frac{P_{s r}\left(W_{i}-2\right)}{L_{T}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{4.41}
\end{equation*}
$$

The $S N R$ according to Eq. (2.29), can be given as,

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s r}\left(W_{i}-2\right)}{L_{T}}\right)^{2}}{e B \mathcal{R}\left[\frac{P_{s r}\left(W_{i}-2\right)}{L_{T}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}}} \tag{4.42}
\end{equation*}
$$

The $B E R$ is described as given in Eq. 2.31.

### 4.4 Numerical Results

Parameters used to obtain numerical results are given in Table 4.2. Higher weight, medium weight, and lower weight are denoted as $W_{H}, W_{M}$ and $W_{L}$ respectively. For each weight, numbers of users are considered to be 50. Data

Table 4.2: The Parameters used to find out the numerical results for VW code.

| Parameters | Values |
| :---: | :---: |
| Broadband source linewidth $(\Delta v)$ | 3.75 THz |
| Electrical bandwidth $(\mathrm{B})$ | 311 MHz |
| Effective power of broadband $\left(P_{s r}\right)$ | -10 dBm |
| Quantum efficiency $(\eta)$ | 0.6 |
| Operating wavelength $\left(\lambda_{0}\right)$ | 1550 nm |
| Receiver noise temperature | 300 K |
| Receiver Load resistor | $1030 \Omega$ |
| Electron charge $(e)$ | $1.6 \times 10^{-19} \mathrm{C}$ |
| Planck's constant $(\mathrm{h})$ | $6.66 \times 10^{-34} \mathrm{~J} / \mathrm{s}$ |
| Boltzmann's constant $\left(K_{b}\right)$ | $1.38 \times 10^{-23} \mathrm{~J} / \mathrm{K}$ |

rate is chosen as 622 Mbps to compare with existing literature.
In Fig. 4.2, BER is plotted against number of users for proposed VW code with ( $W_{L}=4$ and $W_{H}=6$ ), VW KS code with ( $W_{L}=4$ and $W_{H}=6$ ) and RD code with ( $W_{L}=5$ and $W_{H}=13$ ). All the compared codes use BD technique.

BD technique describes reduction of MAI using the IPCC codes [20].
KS code is designed only for even weights. It uses mapping to give more codes for same weight and variable weight. RD code is designed for weight greater than 2. It uses two segments code and data. Data segment has zero cross correlation. The code segment is responsible for cross correlation and its value is high. To obtain the codes for variable weight, RD code uses the mapping technique. Mapping technique can efficiently use the available bandwidth, only if number of requesting users are same as maximum generated users. Otherwise, some portion of the bandwidth may be left unused and result in an increased code length [45].

In comparison to other codes, proposed VW code is applicable for any


Figure 4.2: Comparison of proposed VW code with other codes using BD technique.
number of users with weight greater than 2. It does not use mapping technique to obtain more codes. A single algorithm is used for variable weights higher than two. It gives comparable, or better $B E R$ performance than others, and effect of mapping [86] on $B E R$ is eliminated. Supportable number of users for higher weight, at $B E R$ of $10^{-9}$ (data) are 28,33 and 35 for RD code, KS code, and VW code respectively. Supportable number of users for lower weight, at $B E R$ of $10^{-4}$ (voice) are 23, 31 and 37 for RD code, KS code, and VW code respectively.

Figure 4.3 shows $B E R$ versus number of users for VW code by varying the higher weight and keeping lower weight fixed. The combination of two weights $\left(W_{H}, W_{L}\right)$ is taken as $(6,4),(5,4)$ and $(7,4)$.

The larger value of $W_{H}$ tends to increase code length and decrease the $B E R$ of users. Increasing $W_{H}$ increases the total code length which leads to higher the $B E R$ at fixed $W_{L}$. At $B E R$ of $10^{-4}$, supportable number of users are $50,36,16$ for $W_{L}=4$ when $W_{H}$ is 7,6 and 5 respectively. At $B E R$ of $10^{-9}$, supportable number of users are $41,35,26$ for $W_{L}=4$ when $W_{H}$ is 7,6


Figure 4.3: Performance of proposed VW code on varying the higher weight $\left(W_{H}\right)$ and fixed lower weight $\left(W_{L}\right)$.
and 5 respectively.
In Fig. 4.4, $B E R$ is plotted against number of users for varying $W_{L}$ and fixed $W_{H}$. The combinations of two weights $\left(W_{H}, W_{L}\right)$ are taken as $(6,5),(6,4)$ and $(6,3)$. As $W_{L}$ is increased, $B E R$ and code length of system decreased and increased respectively. Increasing $W_{L}$ increases total code length, resulting in higher $B E R$ for $W_{H}$ users.

The higher $W_{L}$ tends to increase the code length which increases the required total code length of $W_{H}$. Hence, lowering the performance of fixed $W_{H}$ for increasing $W_{L}$. The supportable number of users are 50,36 , and 30 at $B E R$ of $10^{-3}$ for $W_{L}=5,4$ and 3 respectively. The supportable number of users for $W_{H}$ are 44,35 and 25 at $B E R$ of $10^{-9}$ on varying $W_{L}=5,4$ and 3 , respectively.

From Eq. (4.32), both numerator and denominator have term $\left(1 / L_{T}\right)$. On multiplying $L_{T}^{2}$ to numerator and denominator in Eq. (4.32), denominator varies quadratically with ${ }^{\prime} L_{T}^{\prime}$. Hence, increase in $L_{T}$ reduces SNR leading to higher $B E R$.


Figure 4.4: Performance variation of proposed VW code on varying the lower weight $\left(W_{L}\right)$ and taking higher weight $\left(W_{H}\right)$ fixed.

Figures 4.5 and 4.6 use three different weights combination corresponding to $W_{H}=6, W_{M}=5$, and $W_{L}=3$. Figure 4.5 illustrates the $B E R$ for users with $W_{H}, W_{M}$, and $W_{L}$ versus number of users (each weight) using proposed VW code. The number of users for each weight is chosen as 40. Figure 4.5 also presents the comparison between BD and DD techniques. It is plotted between $B E R$ versus number of users. The maximum number of supportable users are 40,40 and 40 for voice $\left(10^{-3}\right)$, data $\left(10^{-9}\right)$ and video $\left(10^{-12}\right)$, respectively using DD detection. Whereas for BD detection, maximum number of supportable users are 40,0 and 5 for voice $\left(10^{-3}\right)$, data $\left(10^{-9}\right)$ and video $\left(10^{-12}\right)$, respectively. Since PIIN is not considered in DD , performance is better with respect to BD technique. In DD technique, the receiver is designed with less complexity and its cost is reduced along with better performance $[43,86]$. Figure 4.6 illustrates the $B E R$ (PIIN, Shot and thermal noise) versus received power using balanced detection for $W_{H}=6, W_{M}=5, W_{L}=3$ with 25 users for each weight. $B E R$ of all users decreases with the increase of weight and received power. The application of


Figure 4.5: Comparison of BD and DD techniques for proposed VW code ( $W_{H}=6, W_{M}=5, W_{L}=3$ ).
proposed VW code to support different services, for average received power of -20 dBm has acceptable performance.

It is found that proposed VW code gives comparable and better performance than Generalized Optical Code construction for Enhanced and Modified Double Weight code (Constant weight constant length construction). That is due to lower code length of variable weight codes.

### 4.5 Summary

VW algorithm is proposed for generalized optical code for enhanced and Modified Double Weight. It is designed for any number of users for weight greater than 2. It does not use mapping technique to obtain more users. The cross correlation of value at most 1 is obtained between any two users. Code construction is begins with the highest weight. On changing number of users of highest weight, code lengths of all lower weight codes are changed. On the other hand, changing number of users of lowest weight, affects its own


Figure 4.6: Comparison of received power for proposed VW code ( $W_{H}=$ $6, W_{M}=5, W_{L}=3$ ) considering PIIN, shot and thermal noise.
code length and total code length, but does not affect codes of other higher weights. The variation of weights provides different $B E R$. The lowest weight codes have highest $B E R$ and highest weight codes have lowest $B E R$.

CHAPTER

## A new code construction algorithm based on Double Weight Codes with mapping

### 5.1 Introduction

Reported DW codes algorithms construct the codes on designing different basic matrix of individual weights (odd, even, and 2), and codes for total $N$ number of users are constructed by using mapping. In Chapters 3 and 4, algorithms are proposed without mapping for weights greater than 2. This Chapter describes the effect of mapping and construction of the single code algorithms with mapping for all weights. Like DW code families, basic matrix is first constructed using proposed algorithm. The number of users for basic code matrix depends on the code weight and on a constant value. As size
of basic matrix is changed, $B E R$ and code length of users are changed. The properties of proposed code are:

- Easy code construction.
- Crosscorreation is $\lambda_{c} \leq 1$.
- Any positive integer weight can be used for code construction.
- Variety of code set is constructed.
- Size of basic matrix is chosen according to code performance.

2D code construct is also constructed by using 1D code construction. 2D code gives better performance with higher number of users compare to 1D code.

### 5.2 1D Code Construction

### 5.2.1 Algorithm

Code construction is starts with constructing the basic matrix ( $M$ ) of size $\left(N_{B} \times L_{B}\right)$. Here, $N_{B}$ shows number of users at basic matrix, and it is defined using two conditions for all weights $W$.

$$
N_{B}= \begin{cases}3, & \text { A constant value }  \tag{5.1}\\ W, & \text { Depend on } W\end{cases}
$$

$L_{B}$ is the code length given for basic matrix, defined as

$$
\begin{equation*}
L_{B}=\sum_{i=1}^{W} i=W(W+1) / 2 . \tag{5.2}
\end{equation*}
$$

As describe in [58], $P_{n}$ denotes the position of $n^{\text {th }}$ pulse in the code sequence for basic matrix and is given by

$$
P_{n}=\left\{\begin{array}{ll}
1, & n=1  \tag{5.3}\\
P_{n-1}+(n-1), & n>1
\end{array} .\right.
$$

Where, $n$ denotes $n \in 1,2, \ldots, W$. Codes for $N$ users are assigned by repeating basic matrix $Z$ times diagonally, where $Z$ is given by

$$
\begin{equation*}
Z=\left\lfloor N / N_{B}\right\rfloor . \tag{5.4}
\end{equation*}
$$

As defined in [58], Code length $(L)$ for $N$ users is given by

$$
\begin{equation*}
L=Z \times L_{B} . \tag{5.5}
\end{equation*}
$$

The complete code matrix consisting of $N$ users is written in Eq. (2.2).
Algorithm implementation steps:
Step 1: Define parameters

1. Define $W, N_{B}$ and $N$.
2. Calculate $L_{B}$ and $L$ as defined in Eqs. (5.2) and (5.5) respectively.

Step 2: Construct the basic matrix.

1. Generate a code sequence using Eq. (5.3) and by filling empty spaces with zeros.
2. Rotate code sequence right by one position upto $N_{B}-1$ times.
3. Each rotation generates a code sequence.
4. Arrange the generated code sequences in matrix form.
5. After second rotation, find the sum of each column in matrix for each rotation.
6. If all sums are less than 3, codes are generated
7. If sum is greater than 2 , interchange the pulse position $\left(P_{n}\right)$ of that column with zero of the column which has sum less than 2 in a same row.
8. Generated matrix is called as basic matrix ( $M$ ).

Step3 : All $N$ users codes are constructed by using mapping ( $Z$ times repetition of basic matrix) as given in Eq. (2.2).

### 5.2.2 Code construction examples

Example 1 For $W=2$ and $N_{B}=3$ (Constant)
Step 1: Define parameters.

1. $L_{B}=\sum_{i=1}^{2} i=3$.
2. Let $N=12$ and calculated value of $L=12$.

Step 2: Construction of basic matrix.

1. Calculate the ones positions for given $W$ as

$$
P_{n}=\left\{\begin{array}{l}
P_{1}=1, \\
P_{2}=P_{2-1}+(2-1)=2,
\end{array}\right.
$$

2. Arrange these ones to from a code and the empty spaces by zero as

$$
\text { Code1 }\left[\begin{array}{ccc}
1 & 1 & . . \\
1 & 1 & 0 \\
P_{1} & P_{2} &
\end{array}\right] .
$$

Generated code is denoted by code1.
3. Rotate code1 right by $N_{B}-1=2$.
4. Rotate code 1 right by one position.

$$
\text { Code2 } \quad\left[\begin{array}{lll}
0 & 1 & 1
\end{array}\right] .
$$

5. Rotate code2 right by one position.

$$
\text { Code3 } \quad\left[\begin{array}{lll}
1 & 0 & 1
\end{array}\right] .
$$

6. Arrange all the generated codes in matrix form. Check whether all column sums are less than 3 or not.
Code1
Code2
Code3
Sum $\left[\begin{array}{lll}1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ \hline 2 & 2 & 2\end{array}\right]$

Basic matrix for $N_{B}=3$ is generated.

Step3: The basic matrix is repeated diagonally for $Z=4$ as given in Eq. (2.2).

## Example 2 for $W=2$ and $N_{B}=2$

Step 1: Define parameters.

1. $L_{B}=\sum_{i=1}^{2} i=3$.
2. Let $N=12$ and calculated $L=18$.

Step 2: Construction of basic matrix is same as describe in step 2 from 1 to 4.

1. Arrange all the generated codes in matrix form. Check whether all

column sums are less than 3 or not. | Code1 |
| :---: |
| $\operatorname{Code2}$ |
| Sum |\(\left[\begin{array}{ccc}1 \& 1 \& 0 <br>

0 \& 1 \& 1 <br>
\hline 1 \& 2 \& 1\end{array}\right]\) Basic matrix for $N_{B}=2$ is generated.

Step3: The basic matrix is repeated diagonally for $Z=3$ as given in Eq. (2.2).

### 5.2.3 $B E R$ analysis

Let $C_{k}(j)$ be the $j$ th element of the $k$ th proposed code. At balanced receiver, upper part which has same wavelength structure as encoder has correlation function as

$$
\sum_{j=1}^{L} C_{k}(j) \cdot C_{l}(j)=\left\{\begin{array}{ccc}
W & k=l & \text { same user inside } M  \tag{5.6}\\
1 & k \neq l & \text { other users inside } M \\
0 & k \neq l & \text { other users outside } M
\end{array}\right.
$$

For given user, autocorrelation is $W$. Cross correlation is 1 and 0 for within $M$ and outside $M$ respectively. In case of lower arm, cross correlation function is defined as

1. Ex-ORing desired user with interfering user.

$$
C_{Z}(j)=\sum_{j=1}^{L} C_{k}(j) \oplus C_{l}(j)
$$

$\oplus$ denotes the Ex-OR function.
2. $C_{Z}$ is $A N D$ with given interfering user [57].

$$
C_{Y}(j)=C_{Z}(j) \cdot C_{l}(j)
$$

- denotes the $A N D$ function.

3. 

$$
C_{Y}(j)=\left\{\begin{array}{ccl}
0 & k=l & \text { same user inside } M \\
(W-1) & k \neq l & \text { same users inside } M \\
0 & k \neq l & \text { other users outside } M
\end{array}\right.
$$

4. Correlation function is given as

$$
\frac{\sum_{j=1}^{L} C_{k}(j) \cdot C_{Y}(j)}{(W-1)}=\left\{\begin{array}{lll}
0 & k=l & \text { same user inside } M  \tag{5.7}\\
1 & k \neq l & \text { same users inside } M \\
0 & k \neq l & \text { other users outside } M
\end{array}\right.
$$

To analyse $B E R$, the Gaussian approximation with assumptions are taken as per given in [18]. The coherence time of a thermal source [18] is given in Eq. (2.9). The variance of photocurrent [24] can be written as given in Eq. (2.10).

The PSD of the received signals is written as given in Eq. (2.14). The total power at photodetector, $P D_{1}$ of $k$ th receiver $[25,58]$ is

$$
\begin{gather*}
P\left(P D_{1}\right)=\int_{0}^{\infty} G_{1}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{l}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v \\
=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{l}(j) . \tag{5.8}
\end{gather*}
$$

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Using correlation function from Eq. (5.6), Eq. (5.8) is written as

$$
\begin{equation*}
P\left(P D_{1}\right)=\frac{P_{s r} W}{L}+\frac{P_{s r}}{L} \sum_{k=1, k \neq l}^{N_{B}} d_{k} . \tag{5.9}
\end{equation*}
$$

The total power at photodetector, $P D_{2}[25,58]$ is given as

$$
\begin{gather*}
P\left(P D_{2}\right)=\int_{0}^{\infty} G_{2}(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{X}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v \\
P\left(P D_{2}\right)=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N_{B}} d_{k} \sum_{j=1}^{L} C_{k}(j) C_{X}(j) \tag{5.10}
\end{gather*}
$$

Using correlation property given in Eq. (5.7), Eq. (5.10) lead to

$$
\begin{equation*}
P\left(P D_{2}\right)=\frac{P_{s r}}{L} \sum_{k=1, k \neq l}^{N_{B}} d_{k} \tag{5.11}
\end{equation*}
$$

The received signal is the difference between photocurrents, which is expressed as $I=I_{1}-I_{2} . I_{1}$ and $I_{2}$ are currents at photodiodes.

$$
\begin{equation*}
I=\mathcal{R} P\left(P D_{1}\right)-\mathcal{R} P\left(P D_{2}\right) \tag{5.12}
\end{equation*}
$$

Substituting the expressions of $P\left(P D_{1}\right)$ and $P\left(P D_{2}\right)$ of total power incident at input of $P D_{1}$ and $P D_{2}$ from Eqs. (5.9) and (5.11) into Eq. (5.12), the received signal is

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r} W}{L} \tag{5.13}
\end{equation*}
$$

The shot noise is written by substituting Eqs. (5.9) and (5.11) in Eq. (3.17) as

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}\left(W+2\left(N_{B}-1\right)\right)}{L} \tag{5.14}
\end{equation*}
$$

Using approximation as given in Eq. (3.19) and by substituting Eqs. (5.9) and (5.11) in Eq. (3.20), PIIN is expressed as

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2} N W}{L^{2} \Delta v}\left[W+2\left(N_{B}-1\right)\right] \tag{5.15}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ as given in Eq. (2.10) is expressed as

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{2 e B \mathcal{R} P_{s r}\left(W+2\left(N_{B}-1\right)\right)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W\left(W+2\left(N_{B}-1\right)\right)}{L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}} . \tag{5.16}
\end{equation*}
$$

The probability of sending bit 1 is half $[58,86]$, Eq. (5.16) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{P_{s r} e B \mathcal{R}\left(W+2\left(N_{B}-1\right)\right)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W\left[W+2\left(N_{B}-1\right)\right]}{2 L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{5.17}
\end{equation*}
$$

The SNR is given in Eq. (2.29). Put values from Eqs. (5.13) and (5.17) in Eq. (2.29), $S N R$ is

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s r} W}{L}\right)^{2}}{\frac{P_{s r} e B \mathcal{R}\left(W+2\left(N_{B}-1\right)\right)}{L}+\frac{B \mathcal{R}^{2} P_{s r}^{2} N W\left[W+2\left(N_{B}-1\right)\right]}{2 L^{2} \Delta v}+\frac{4 K_{b} T_{n} B}{R_{L}}} . \tag{5.18}
\end{equation*}
$$

The $B E R$ is explained in Eq. (2.31).

### 5.2.4 Numerical Results

Numerical results are simulated using Matlab software. The parameters are given in Table 2.2 to calculate the numerical results. The data rate and maximum number of users are chosen to 622 Mbps and 100 for all simulations respectively.

Figure 5.1 depicts the $B E R$ versus code length for EDW code ( $W=3$ ), proposed code for ( $W=2$ and 3 ) for a condition of $N_{B}=3$ using balanced detection. Proposed code $\left(W=2, N_{B}=3, L_{B}=3\right)$ require less code length



Figure 5.1: $B E R$ versus code length Figure 5.2: Code length against numfor proposed code ( $W=2,3$ ) and ber of users for proposed code and EDW code $(W=3)$ for $N_{B}=3$ upto EDW code for $N_{B}=3, W=3$. 100 users.



Figure 5.3: $\quad B E R$ against code Figure 5.4: $B E R$ against number of length for proposed code when users for proposed code when weight is weight is varied from 2 to 4 for $N_{B}=$ varied from 2 to 4 for $N_{B}=W$ upto $W$ upto 100 users.

100 users.
compare to EDW and proposed code $\left(W=3, N_{B}=3, L_{B}=6\right)$. Reason behind is lower size of basic matrix in case of proposed code ( $W=2, N_{B}=$ $3, L_{B}=3$ ) compare to others Code length of 200, 198 and 99 is required by EDW code, proposed code ( $W=3, N_{B}=3, L_{B}=6$ ) and proposed code ( $W=2, N_{B}=3, L_{B}=3$ ) respectively.

Code length increment of EDW code is differing from proposed code. The difference is shown in Fig. 5.2, for weight $(W=3)$ and basic matrix of $\left(N_{B}=3, L_{B}=6\right)$. Difference in the length is due to different techniques

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used to calculate code length $(L)$ for N users. For EDW, it involves a sine relation between $L$ and $N$ [31]. Proposed code follows constant variation of code length defined in eq. 5.27. These code length variations effect the $B E R$ performance of codes which depend on $N$ and $L$.


Figure 5.5: $B E R$ against number of users for proposed code when weight is varied from 2 to 4 for $N_{B}=3$ upto 100 users.


Figure 5.6: $B E R$ against code length for proposed code when weight is varied from 2 to 4 for $N_{B}=3$ upto 100 users.
$B E R$ is plotted against code length for proposed code when weight is varied from 2 to 4 for a condition of $N_{B}=W$ as shown in Fig.5.3. As the weight $W$ of the proposed code is increased, $N_{B}$ and $L_{B}$ is increased which further increases the size of the basic matrix (in term of $N_{B}$ and $L_{B}$ ). Due to these reasons, code length require for $N$ users are increased as $W$ is increased. Required code length $(L)$ for $W=2,3$ and 4 are 150, 198 and 250 respectively.

Figure 5.4 depicts the $B E R$ againstnumber of users for proposed code when weight is varied from 2 to 4 for a condition of $N_{B}=W$. As $W$ of proposed code is increased, the number of users $\left(N_{B}\right)$ at basic matrix is increased. Increase in $N_{B}$, increase the interfering users at basic matrix which decreases the $B E R$ performances. For proposed code with $W=2,3$ and 4 , number of users are 87,75 and 70 respectively.

Figure 5.5 depicts $B E R$ against number of users for proposed code when $W=4,3$ and 2 at constant value of $N_{B}=3 . L_{B}$ of basic matrix is increased as $W$ is increased and $N_{B}$ is fixed to value 3 for all weights. Because of above reason interfering users in basic matrix is fixed and on other hand weight and code length of each user is increased. Due to these facts, $B E R$ performance is improved as weight increases.

Figure 5.6 illustrates the $B E R$ against code length for proposed code when $W=4,3$ and 2 for $N_{B}=3$. The code length $L$ depends on $L_{B}, N_{B}$ and $N . L_{B}$ increases as weight $W$ of code increases. For $N_{B}=3$ condition, code length for $W=2,3$ and 4 are 99, 198 and 330 respectively.

As weight $(W)$ of proposed code is changed, $M$ and $L$ are changed in a two ways. First way is the $N_{B}$ is constant $\left(N_{B}=3\right)$ and $L_{B}$ is increased as $W$ is increased. Second way is both $N_{B}=W$ and $L_{B}$ are increased as $W$ is increased. Due to above conditions, repetition of basic matrix $(M)$ is changed. Resultant code length required for $N$ users is changed.

### 5.3 2D code construction

### 5.3.1 Algorithm

2D Code construction begins with construction of basic matrix of size ( $N_{g} \times$ $L_{x}$ ) for 1D code. $N_{g}$ is the number of users in basic matrix, and is equal to $W_{x} . W_{x}$ is code weight of spectral dimension. $L_{x}$ is the code length for basic matrix, and it is defined as

$$
\begin{equation*}
L_{x}=W_{x}\left(W_{x}+1\right) / 2 \tag{5.19}
\end{equation*}
$$

As described in [58], $P_{n}$ denotes the position of $n^{\text {th }}$ pulse in the code
sequence for basic matrix and as given in Eq. (5.3).
Spatial dimension is derived as. The basic matrix of size $\left(N_{h} \times L_{y}\right)$. Where $N_{h}$ is the number of users in basic matrix, and is equal to $N_{g}$. Code weight $W_{y}$ is given as

$$
\begin{equation*}
W_{y}=W_{x}-1 \tag{5.20}
\end{equation*}
$$

Code length $\left(L_{y}\right)$ is given as

$$
\begin{equation*}
L_{y}=N_{h} \times W_{y} . \tag{5.21}
\end{equation*}
$$

For second dimension, code construction is explained as Subtracting the positions of $P_{n+1}$ from $P_{1}$ code as

$$
\begin{equation*}
P_{m}=P_{n+1}-P_{1} . \tag{5.22}
\end{equation*}
$$

Where $P_{m}$ is the position of ones in spatial dimension and, $\mathrm{n}=1,2, \ldots$
Total number of codes for $N$ users is given as

$$
\begin{equation*}
N=g \times h . \tag{5.23}
\end{equation*}
$$

Where $g$ and $h$ are number of codes used for each dimension. These codes are assigned by repeating basic matrix diagonally $M_{g}$ and $M_{h}$ times. $M_{g}$ and $M_{h}$ are given as

$$
\begin{equation*}
M_{g}=\left\lfloor g / N_{g}\right\rfloor \tag{5.24}
\end{equation*}
$$

and

$$
\begin{equation*}
M_{h}=\left\lfloor h / N_{h}\right\rfloor . \tag{5.25}
\end{equation*}
$$

As defined in [58], code length $\left(L_{g}\right.$ and $\left.L_{h}\right)$ for $g$ and $h$ codes are given by

$$
\begin{equation*}
L_{g}=M_{g} \times L_{x} \tag{5.26}
\end{equation*}
$$

and

$$
\begin{equation*}
L_{h}=M_{h} \times L_{y} . \tag{5.27}
\end{equation*}
$$

Algorithm implementation steps:
Step 1: Define parameters

1. Choose $W_{x}$.
2. Calculate $L_{x}, W_{y}, L_{y}$, and $N$ as defined in Eqs. (5.19), (5.20), (5.21) and (5.23) respectively.
3. $N_{h}$ and $N_{g}$ are equal to $W_{x}$.

Step 2: Construct the code for spectral dimension.

1. Generate code sequence using Eq. (5.3) and by filling empty spaces with zeros.
2. Rotate code sequence right by one position upto $N_{g}-1$ times and each rotation generates a code sequence.
3. Arrange the generated code sequences in matrix form.
4. After second rotation, find the sum of each column in matrix for each rotation.
5. If all sums are less than 3, codes are generated
6. If sum is greater than 2 , interchange the pulse position $\left(P_{n}\right)$ of that column with zero of the column which has sum less than 2 in a same row.

Table 5.1: 2D code construction using DW codes.

|  | $\left[\begin{array}{lllllll} & 1 & 0\end{array}\right.$ | $\left[\begin{array}{llllll} & 1 & 1\end{array}\right.$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 1 | 1 | 0 | 0 | 1 | 1 |  |
| 1 | 1 | 1 | 0 | 0 | 1 | 1 |  |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| 1 | 1 | 1 | 0 | 0 | 1 | 1 |  |
| 1 | 1 | 1 | 0 | 0 | 1 | 1 |  |

Table 5.2: 2 D code cross corelation values

|  | $R^{0}(g, h)$ | $R^{1}(g, h)$ | $R^{2}(g, h)$ | $R^{3}(g, h)$ |
| :--- | :---: | :---: | :---: | :---: |
| $g=0 \bigcap h=0$ | $W_{x} W_{y}$ | 0 | 0 | 0 |
| $g=0 \bigcap h \neq 0$ | $W_{x}$ | $W_{x}$ | 0 | 0 |
| $g \neq 0 \bigcap h=0$ | 0 | 0 | $W_{y}$ | 0 |
| $g \neq 0 \bigcap h \neq 0$ | 0 | 0 | 1 | 1 |

7. Generated matrix is called as basic matrix $\left(C_{g}\right)$, and is repeated diagonally $M_{g}$ times, to construct the code for all $g$.

Step 3: Construct the code for second dimension.

1. Generate code sequence using Eq. (5.22) and filling empty spaces with zeros.
2. Rotate code sequence right by one position upto $N_{g}-1$ times. Each rotation generates a code sequence.
3. After second rotation, find the sum of each column in matrix for each rotation.
4. If all sums are one, codes are generated
5. If sum is greater than 1 , interchange the pulse position $\left(P_{m}\right)$ of that column with zero of the column in same row.
6. Generated matrix is called as basic matrix $\left(C_{h}\right)$, and is repeated diagonally $M_{h}$ times, to construct the code for all $h$.

Example-
Step 1: Define parameters-

1. $W_{x}=2$.
2. $W_{y}=W_{x}-1=1, N_{g}=2=N_{h}, L_{x}=(2 * 3) / 2=3$ and $L_{y}=2$.

Step 2:

1. $P_{1}=1$, (first one is at position 1 )
2. $P_{2}=P_{2-1}+(2-1)=2$, $($ second one is at position 2$)$
3. Arrange these ones to from a code as

1 1... .
4. Fill the empty spaces by zero $\left[\begin{array}{lll}1 & 1 & 0\end{array}\right]$.
5. Generated code for user 1 is denoted by code 1 .
6. Rotate code 1 right by one position upto given number of ( $N_{g}-1=1$ ). Code 2 is generated $\left[\begin{array}{lll}0 & 1 & 1\end{array}\right]$.
7. Put all the generated codes in matrix form to find the sum of each column, and check whether it is greater than two or not. If it is greater than 2 , interchange the 1 of that column with zero of the column for same row which has sum less than 2 as shown below

$$
\left[\begin{array}{ccc}
1 & 1 & 0 \\
0 & 1 & 1 \\
\hline 1 & 2 & 1
\end{array}\right] \quad \begin{gathered}
\text { Code 1 } \\
\text { Code } 2 \\
\text { Sum }
\end{gathered}
$$

Step 3:

1. From code 1, on subtracting the positions of $n+1$ from $P_{1}$ code for another dimension is drived. $P_{n+1}-P_{1}=P_{m}$

$$
P_{1}=P_{2}-P_{1}=1
$$



Figure 5.7: SAC-OCDMA network design using 2D code.
2. Arrange these ones to from a code as 1 ... .
3. Fill the empty spaces by zeros

10 code 1 .
4. Rotate code 1 right by one position upto given number of $\left(N_{g}-1=2\right)$.

Code 2 is generated $\left[\begin{array}{ll}0 & 1\end{array}\right]$.
\(\left[\begin{array}{ll}1 \& 0 <br>
0 \& 1 <br>

\hline 1 \& 1\end{array}\right] \quad\)| Code 1 |
| :---: |
| Code 2 |
| Sum |

The cross correlation of 2D code is calculated as

$$
\begin{equation*}
R_{g h}^{(d)}=\sum_{i=o}^{L_{g}-1} \sum_{j=0}^{L_{h}-1} C^{(d)} C_{g h} . \tag{5.28}
\end{equation*}
$$

Where $C^{(d)}$ denotes characteristic matrices $d(0,1,2,3), C^{0}=X_{g}^{T} Y_{h}, C^{1}=$ $\overline{X_{g}^{T}} Y_{h}, C^{2}=X_{g}^{T} \overline{Y_{h}}$, and $C^{3}=\overline{X_{g}^{T}} \overline{Y_{h}} . T$ denotes the transpose function. $\overline{X_{g}^{T}}$ and $\overline{Y_{h}}$ are complement of $X_{g}$ and $Y_{h} . C_{g h}$ is total number of codes, given as $X_{g}^{T} Y_{h}$. Here, $X_{g}$ and $Y_{h}$ are 1D codes in spectral and spatial domain respectively. Codes are represented as $X=x_{0}, x_{1}, x_{2}, \ldots \ldots, x_{L_{g}-1}$ and $Y=$ $y_{0}, y_{1}, y_{2}, \ldots . ., y_{L_{h}-1} . L_{g}$ and $L_{h}$ are code lengths of 1D code.

The MAI elimination is obtained as follows using Table 5.2

$$
R_{g, h}^{(0)}-\frac{R_{g, h}^{(1)}}{\left(W_{x}-1\right)}=\left\{\begin{array}{cc}
W_{x} W_{y} & \text { same user or } \mathrm{g}=0, \mathrm{~h}=0  \tag{5.29}\\
0 & \text { other users }
\end{array}\right.
$$



Figure 5.8: Encoder design using 2D Figure 5.9: Decoder structure using code.
2D code.

### 5.3.2 System Description

Figure 5.7 shows the SAC-OCDMA system implementation using 2D code. System consists of $g \times h$ pairs of transmitters and receivers. There are $h$ star couplers with $g \times h$ inputs and $g \times h$ outputs. The structure of transmitter for
each user is shown in Fig. 5.8. At the transmitter, Broadband Source (BBS) is modulated according to incoming data. The spectral encoding of code is done by selecting wavelengths using Fiber Bragg Grating (FBGs) according to the spectral code. Optical splitter is used to provide spatial encoding after spectral encoding. It divides each spectral component equally. Output of splitter is sent towards the $h$ star couplers.

Figure 5.9 shows the structure of the receiver. Output from $h$ star couplers are received and combined by two combiners. Upper and lower combiners outputs correspond to the spatial code. FBGs are designed according to the spectral code sequence. Upper FBG is used to obtain the spectral components, which are matched to 1 s of the spectral code sequence. Lower FBG is used to obtain the spectral components, which are matched to 0s of the spectral code sequence means complement of code. The optical attenuator with the value of $1 / W_{x}-1$ is used to adjust the power level of the optical pulses.
$P D 0$ and $P D 1$ convert the optical signals to electronic signals and then pass them to the integrator. The output current from $P D 0$ and $P D 1$ are proportional to $R_{g, h}^{(0)}$ and $R_{g, h}^{(1)} /\left(W_{x}-1\right)$ respectively. The output current at the integrator is proportional to $R_{g, h}^{(0)}-R_{g, h}^{(1)} /\left(W_{x}-1\right)$. The value of output current is equal to $W_{x} W_{y}$ for same user $g=h=0$, or zero for other users, according to Eq. 5.29.

### 5.3.3 $B E R$ analysis

To analyse BER of the system, the Gaussian approximation as in Section 2.3.1, the coherence time of a thermal source [18] as given in Eq. (2.9) and The variance of photocurrent [24] as given in Eq. (2.10) are considered for
analysis. The PSD of the received optical signals can be written as

$$
\begin{equation*}
r(f)=\frac{P_{s r}}{K_{y} \Delta f} \sum_{U=1}^{U} d(u) \sum_{i=0}^{\left(L_{x}-1\right)} \sum_{j=0}^{\left(L_{y}-1\right)} a_{i j}(u) F(f, i) \tag{5.30}
\end{equation*}
$$

Here $d(u)$ is the data bit of the $u$ th user, $P_{s r}$ is effective power of a BLS at the receiver, $a_{i, j}(u)$ is element of $u$ th user code and $F(f, i)$ is explained in terms of unit step function $u(f)$ as shown in Eqs.(5.31).

$$
\begin{align*}
& F(f, i)=u\left[f-f_{0}-\frac{\Delta f}{2 L_{x}}\left(-L_{x}+2 i\right)\right] \\
&-u\left[f-f_{0}-\frac{\Delta f}{2 L_{x}}\left(-L_{x}+2 i+2\right)\right] \tag{5.31}
\end{align*}
$$

PSDs of received signals at PDs of each user can be written as

$$
\begin{align*}
& S_{0}(f)=\frac{P_{s r}}{W_{h} \Delta f} \sum_{n=1}^{N} d(n) \sum_{i=0}^{L_{g}-1} \sum_{j=0}^{L_{h}-1} a_{i j}^{(0)} a_{i j}(u) * F(f, i)  \tag{5.32}\\
& S_{1}(f)=\frac{P_{s r}}{W_{h} \Delta f} \sum_{n=1}^{N} d(n) \sum_{i=0}^{L_{g}-1} \sum_{j=0}^{L_{h}-1} a_{i j}^{(1)} a_{i j}(u) * F(f, i) \tag{5.33}
\end{align*}
$$

Calculate the output currents of each PDs as

$$
\begin{array}{r}
I_{0}=\mathcal{R} \int_{0}^{\infty} S_{0}(f) d f=\frac{\mathcal{R} P_{s r}}{W_{h} L_{g}}\left[W_{g} W_{h}+\frac{W_{h}(N-1)\left(N_{g}-1\right)}{(g h-1)}\right] \\
I_{1}=\mathcal{R} \int_{0}^{\infty} S_{1}(f) d f=\frac{\mathcal{R} P_{s r}}{W_{h} L_{g}}\left[\frac{W_{h}(N-1)\left(N_{g}-1\right)}{(g h-1)}\right] \tag{5.35}
\end{array}
$$

The average photo current of receiver is given as

$$
\begin{equation*}
I=\mathcal{R} \int_{0}^{\infty}\left(S_{0}(f)-S_{1}(f)\right)=I_{0}-I_{1}=\frac{\mathcal{R} P_{s r} W_{g}}{L_{g}} \tag{5.36}
\end{equation*}
$$

The shot noise is

$$
\begin{equation*}
I_{\text {shot }}=2 e B I_{\text {total }}=2 e B\left(I_{0}+I_{1}\right) \tag{5.37}
\end{equation*}
$$

The PIIN is

$$
\begin{gather*}
I_{P I I N}=B I^{2} \tau=B \mathcal{R}^{2} \int_{0}^{\infty}\left[S_{0}-S_{1}\right]^{2} d f  \tag{5.38}\\
I_{P I I N}=B \mathcal{R}^{2} \int_{0}^{\infty}\left[S_{0}^{2}(f)-2 S_{0}(f) S_{1}(f)+S_{1}^{2}(f)\right] d f=\frac{B \mathcal{R}^{2} P_{s r} W_{x}^{2}}{\Delta f L_{x}} \tag{5.39}
\end{gather*}
$$

Each user transmits $1 s$ and $0 s$ with equal probability.

$$
\begin{gather*}
I_{\text {shot }}=e B \frac{\mathcal{R} P_{s r}}{W_{h} L_{g}}\left[W_{g} W_{h}+\frac{2 W_{h}(N-1)\left(N_{g}-1\right)}{(g h-1)}\right]  \tag{5.40}\\
I_{P I I N}=\frac{B \mathcal{R}^{2} P_{s r} W_{x}^{2}}{2 \Delta f L_{x}} \tag{5.41}
\end{gather*}
$$

The $S N R$ is defined in Eq. (2.29). The $B E R$ is calculated by using Gaussian approximation from $S N R$ as expressed in Eq. (2.31).

### 5.3.4 Numerical results

The relevant parameters as given in Table 2.2 are used to obtain numerical results. Figure 5.10 depicts the $B E R$ versus number of users for 1D code for $W=2,2 \mathrm{D}$ hybrid code ( $m_{s}=21, P=7$ ) and 2D code for $(g=7, h=21)$ at a data rate of 5 Gbps using balanced detection. The total number of users for 1 D and 2 D codes are set to 150 . The total number of users for hybrid code is 147 dependent on $\left(m_{s}, P\right)$. The $B E R$ of $4 \times 10^{-6}$ and $9 \times 10^{-15}$ are
obtained using 2D hybrid code and proposed 2D code respectively. The 2D hybrid code is using values of weights $K_{l}=20$ for spectral and $K_{p}=3$ for spatial dimension.

The proposed 2D code is using $W_{x}=2$ for spectral and $W_{y}=1$ for spatial. The 2D hybrid code requires more bandwidth of source compared to proposed 2D code due to higher value of spectral weight. Degradation of $B E R$ performance of 1 D code is fast compared to proposed 2D code as shown in Fig. 5.10.


Figure 5.10: Comparison of 2D Hybrid code and 1D code with designed 2D code for $B E R$ versus number of active users.


Figure 5.12: $B E R$ versus Line Figure 5.13: $B E R$ versus received width of BBS for different value of power when active number of users are $g$ and $h$ for 2D code.


Figure 5.11 depicts the effect of data rate on $B E R$. The weight of the
code is set by values $W_{x}=2, W_{y}=1$. The number of users are chosen to be 200. The number of codes for both dimension are taken as $(g=25, h=8)$, $(g=10, h=20)$, and $(g=5, h=40)$. These codes attain a $B E R$ of $10^{-9}$ at data rate of 6.54 Gbps for $(g=5, h=40), 3.15 \mathrm{Gbps}$ for $(g=10, h=20)$, and 1.14 Gbps for $(g=25, h=8)$. As the value of spatial codes $h$ is increased and spectral codes $g$ is decreased, $B E R$ performance is improved. This is due to orthogonal property of $h$ codes.

Figure 5.12 shows the $B E R$ versus Line width of BBS for different values of $g$ and $h$ for 2D code. The values of $g$ and $h$ are taken as $(g=10, h=20)$, $(g=14, h=10)$, and $(g=20, h=10)$. Data rate of $10 G b p s$ is set for numerical result. The code size $(g=10, h=20)$ requires less line width of source than other two code values. This is due to lower value of spectral code $g$. Lower value of $g$ requires less amount of BBS. Figure 5.13 shows $B E R$ versus received power when active number of users are 200 and data rate is 5 Gbps. The code size of $(g=10, h=20)$ and $(g=20, h=10)$ are used to have 200 users. The lower value of spectral code $g$ require less power compared to higher value of $g$.

### 5.4 Summary

A new and single code construction algorithm is proposed for DW code families for all weights using mapping. Proposed code algorithm is analysed for $B E R$ and compared with EDW code. A other 2D code is proposed for SAC-OCDMA systems. The code is having a low value of IPCC for spectral dimension and orthogonal in spatial dimension. In comparison with 1D code, it offers greater number of users along with better $B E R$ performance.

## CHAPTER <br> 6

## Development of ZCCC for Constant and Variable Weight

### 6.1 Introduction

The codes proposed in Chapters 2, 3, 4 and 5, suffer from PIIN. PIIN is eliminated theoretically by using the codes with zero cross correlation (ZCC) property. The code with the property of zero cross correlation is called Zero Cross Correlation Code (ZCCC). The code structure of ZCCC does not have any overlapping of wavelengths between any users. The ZCC code is reported with Constant Weight (CW) code construction in [36]. Codes are using mapping technique to provide codes for the higher number of users. Basic matrix is constructed by using code transformation technique which needs the basic matrix of all lower weights.

A new ZCCC is proposed without mapping. Code construction algorithm is designed with any weight for any number of users having constant or
variable weights. Variable weight (VW) codes give different QoS, and are suitable, and useful for multimedia applications.

### 6.2 Constant Weight Code Construction

Construction of code is as follows

1. Define weight $W$ and number of users $N$ for code.
2. Basic matrix $M$ of size $2 \times W$ for $W$ is constructed as

$$
M=\left[\begin{array}{l}
S_{1}  \tag{6.1}\\
S_{2}
\end{array}\right]=\left[\begin{array}{ll}
\left\lfloor\frac{W}{2}\right\rfloor 0 s & \left\lfloor\frac{W+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{W}{2}\right\rfloor 1 s & \left\lfloor\frac{W+1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times W}
$$

3. Basic matrix of weight $W$ is repeated $N_{W}+1$ times as

$$
U=\left[\begin{array}{ccccc}
S_{1} & . . & . . & . . & . .  \tag{6.2}\\
S_{2} & S_{1} & . . & . . & . . \\
. . & S_{2} & S_{1} & . . & . . \\
. . & . . & \ddots & . . & . . \\
. . & . . & \ddots & S_{2} & S_{1} \\
\vdots & \vdots & \vdots & \vdots & S_{2}
\end{array}\right] .
$$

4. First and last rows along with unused columns of $U$ matrix are removed. Unused columns are equal to $\left\lfloor\frac{W+1}{2}\right\rfloor+\left\lfloor\frac{W}{2}\right\rfloor$.
5. Code length is calculated as $N * W$.

### 6.2.1 Example

## CW-ZCCC (Proposed)

$W=3$ for $N=3$ are chosen for explanation of code construction and is described below

1. Basic matrix $M$ of size $2 \times 3$ for $W=2$ is constructed as

$$
M=\left[\begin{array}{c}
S_{1}  \tag{6.3}\\
S_{2}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{3}{2}\right\rfloor 0 s & \left\lfloor\frac{3+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{3}{2}\right\rfloor 1 s & \left\lfloor\frac{3+1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times 3}=\left[\begin{array}{ccc}
0 & 1 & 1 \\
1 & 0 & 0
\end{array}\right]_{2 \times 3}
$$

2. Basic matrix is repeated 4 times as

$$
U=\left[\begin{array}{cccc}
011 & . . & . . & . . \\
100 & 011 & . . & . . \\
. . & 100 & 011 & . . \\
. . & . . & 100 & 011 \\
. . & . . & . . & 100
\end{array}\right] .
$$

3. Empty spaces are filled with zeros. First and last rows along with unused columns of $U$ matrix are removed. Unused columns are equal to 3 (shown by parenthesis).

$$
U=\left[\begin{array}{llll}
1(00) & 011 & 000 & (0) 00 \\
0(00) & 100 & 011 & (0) 00 \\
0(00) & 000 & 100 & (0) 11
\end{array}\right]=\left[\begin{array}{llll}
1 & 011 & 000 & 00 \\
0 & 100 & 011 & 00 \\
0 & 000 & 100 & 11
\end{array}\right] .
$$

## ZCC Code (reported)

Basic matrix of size $((W+1) \times W(W+1))$ is first constructed. Basic matrix is repeated diagonally to obtain higher number of users called as mapping. Due to mapping it has a stepwise increase in code length. Basic matrix is obtained by using code transformation technique which need the code of all lower weights [36] e.g. Basic matrix of $(W=3)$ needs basic matrix of $W=1$ and $W=2$.

$$
\text { Basic matrix of }(W=3)=\left[\begin{array}{cccc}
000 & 000 & 010 & 101 \\
000 & 101 & 000 & 010 \\
010 & 010 & 001 & 000 \\
101 & 000 & 100 & 000
\end{array}\right] \text {. }
$$

Proposed ZCCC construct any weight code without any information about lower weight codes. It constructs the code without mapping. It has a linear increase in code length.

### 6.3 Variable Weight Code Construction

Construction of code is as follows

1. The total number of users are defined as

$$
\begin{equation*}
\Psi=\sum_{i=1}^{M} N_{W_{i}} . \tag{6.4}
\end{equation*}
$$

Where $N_{W_{i}}$ users with weight $W_{i}$. Total number of weights are from $W_{1}$ to $W_{M}$.
2. Basic matrix $\left(M_{W_{i}}\right)$ of size $2 \times W_{i}$ for $W_{i}$ is constructed as

$$
M_{W_{i}}=\left[\begin{array}{c}
S_{1}^{\left(W_{i}\right)}  \tag{6.5}\\
S_{2}^{\left(W_{i}\right)}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{W_{i}}{2}\right\rfloor 0 s & \left\lfloor\frac{W_{i}+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{W_{i}}{2}\right\rfloor 1 s & \left\lfloor\frac{W_{i}+1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times W_{i}}
$$

3. Construction of code begins from highest weight $\left(W_{M}\right)$ to lowest weight $\left(W_{1}\right)$.
4. Basic matrix of highest weight $W_{M}$ is repeated $N_{W_{M}}+1$ times as

$$
U=\left[\begin{array}{ccccc}
S_{1}^{\left(W_{M}\right)} & . . & . . & . . & . .  \tag{6.6}\\
S_{2}^{\left(W_{M}\right)} & S_{1}^{\left(W_{M}\right)} & . . & . . & . . \\
. . & S_{2}^{\left(W_{M}\right)} & S_{1}^{\left(W_{M}\right)} & . . & . . \\
. . & . . & \ddots & . . & . . \\
. . & . . & \ddots & S_{2}^{\left(W_{M}\right)} & S_{1}^{\left(W_{M}\right)} \\
\vdots & \vdots & \vdots & \vdots & S_{2}^{\left(W_{M}\right)}
\end{array}\right]
$$

5. For last repeated basic matrix of $W_{M}$, calculate reducibility number $\left(R_{W_{M}}\right)$.
(a) Reducibility number ( $R_{W_{i}}$ ) is defined as given below

$$
\begin{equation*}
R_{W_{i}}=\left\lfloor\frac{W_{i-1}+1}{2}\right\rfloor-\left\lfloor\frac{W_{i}}{2}\right\rfloor \tag{6.7}
\end{equation*}
$$

where $W_{i}$ varies from $W_{M}$ to $W_{1}$.
i. Calculated value of $R_{W_{i}}$ is either 0 or any negative integer value. This is due to code construction which starts from highest weight to lowest weight.
ii. When $R_{W_{i}}=0$, no change is required in basic matrix $M_{W_{i}}$.
iii. When $R_{W_{i}}=$ negative integer, reduce $R_{W_{i}}$ number of 1 s from $S_{2}^{\left(W_{i}\right)}$ and 0 s from $S_{1}^{\left(W_{i}\right)}$ of basic matrix $M_{W_{i}}$.
iv. After reduction, last repeated basic matrix is shown as $\left(S_{1 R}^{\left(W_{i}\right)}, S_{2 R}^{\left(W_{i}\right)}\right)$.
6. Step 4 and 5 are repeated for weights $W_{M-1}$ to $W_{1}$. Basic matrix of $W_{M-1}$ to $W_{1}$ are repeated $N_{W_{M-1}}$ to $N_{W_{1}}$ times respectively as per eq. (6.8).
$U=\left[\begin{array}{cccccccc}S_{1}^{\left(W_{M}\right)} . . & . . \\ & & & & & & \\ S_{2}^{\left(W_{M}\right)} . . & S_{1 R}^{\left(W_{M}\right)} & & & & & & \\ \ldots . & S_{2 R}^{\left(W_{M}\right)} & S_{1}^{\left(W_{(M-1)}\right)} . . & & & & & \\ \vdots & \vdots & S_{2}^{\left(W_{(M-1)}\right)} . . & S_{1 R}^{\left(W_{(M-1)}\right)} & & & & \\ \vdots & \vdots & \vdots & \ddots & & & & \\ \vdots & \vdots & \vdots & \ddots & S_{1 R}^{\left(W_{2}\right)} & & & \\ \vdots & \vdots & \vdots & \vdots & S_{2 R}^{\left(W_{2}\right)} & S_{1}^{\left(W_{1}\right)} & & \\ \vdots & \vdots & \vdots & \vdots & \vdots & S_{2}^{\left(W_{1}\right)} & & \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & & \\ . . & . . & . . & . . & . . & . & S_{2}^{\left(W_{1}\right)} & S_{1}^{\left(W_{1}\right)} \\ . . & . . & . . & . . & . . & . . & . . & S_{2}^{\left(W_{1}\right)}\end{array}\right]$
7. First row and last row of $U$ matrix is removed as shown in eq.(6.9).

$$
U=\left[\begin{array}{cccccccc}
S_{2 R}^{\left(W_{M}\right)} & . . & S_{1 R}^{\left(W_{M}\right)} & & & & &  \tag{6.9}\\
. . & . . & S_{2 R}^{\left(W_{M}\right)} & S_{1}^{\left(W_{(M-1)}\right)} & & & & \\
\vdots & \vdots & \vdots & S_{2}^{\left(W_{(M-1)}\right)} & & & & \\
\vdots & \vdots & \vdots & \vdots & \vdots & \ddots & & \\
\vdots & \vdots & \vdots & \vdots & \ddots & \ddots & S_{1}^{W_{1}} & \\
. . & . . & . . & . . & . . & . . & S_{2}^{W_{1}} & S_{1}^{W_{1}}
\end{array}\right]
$$

8. Empty spaces are filled with zeros.

$$
U=\left[\begin{array}{cccccc}
S_{2}^{\left(W_{M}\right)} . . & S_{1}^{\left(W_{M}\right)} R_{W_{M}} & & & &  \tag{6.10}\\
0 & S_{2}^{\left(W_{M}\right)} R_{W_{M}} & S_{1}^{\left(W_{(M-1)}\right)} . .0 & & & \\
\vdots & \vdots & S_{2}^{\left(W_{(M-1)}\right)} . .0 & & & \\
\vdots & \vdots & \vdots & \ddots & & \\
0 & 0 & 0 & 0 & S_{2}^{W_{1}} & S_{1}^{W_{2}}
\end{array}\right]
$$

9. All 0 s columns are deleted. Number of all 0 s columns are $\left\lfloor\frac{W_{M}+1}{2}\right\rfloor 0 s$ from left side and $\left\lfloor\frac{W_{1}}{2}\right\rfloor 0 s$ from right side.
10. The complete code set is generated as shown in eq.(6.10).
11. At each transition of weight, code length is changed. The code length is amount of Broad Band Source (BBS) (wavelengths) required by a particular weight. Code length $L_{W_{M}}$ is amount of BBS required by $W_{M}$. For $W_{M-1}$, code length $\left(L_{W_{M-1}}\right)$ is ( $L_{W_{M}}+$ BBS required by $W_{M-1}$ ). This is so on upto weight $W_{1}$. Total code length used by the code is $L_{n}$ which is given as

$$
\begin{equation*}
L_{n}=L_{W_{1}} \tag{6.11}
\end{equation*}
$$

where $L_{W_{1}}$ is code length required by weight $W_{1}$.
12. Code lengths are defined as

For $N_{W_{M}}$ users, code length is

$$
\begin{equation*}
L_{W_{M}}=W_{M} *\left(N_{W_{M}}+1\right)+R_{W_{M}}-\left\lfloor\frac{W_{M}+1}{2}\right\rfloor \tag{6.12}
\end{equation*}
$$

For $N_{W_{N-1}}$ users, code length is

$$
\begin{equation*}
L_{W_{M-1}}=L_{W_{M}}+W_{M-1} *\left(N_{W_{M-1}}\right)+R_{W_{M-1}} \tag{6.13}
\end{equation*}
$$

For $N_{W_{N-2}}$ users, code length is

$$
\begin{equation*}
L_{W_{M-2}}=L_{W_{M-1}}+W_{M-2} *\left(N_{W_{M-2}}\right)+R_{W_{M-2}} \tag{6.14}
\end{equation*}
$$

For $N_{W_{1}}$ users, code length is

$$
\begin{equation*}
L_{W_{1}}=L_{W_{2}}+W_{1} *\left(N_{W_{1}}\right)-\left\lfloor\frac{W_{1}}{2}\right\rfloor \tag{6.15}
\end{equation*}
$$

### 6.3.1 Example

$W_{H}=3$ for $N_{H}=3$ and $W_{L}=2$ for $N_{L}=3$ are chosen for explanation of code construction and is described below

1. Size of basic matrix of $W_{H}=3$ is defined as $2 \times 3$ and it is created as

$$
M_{W_{H}}=\left[\begin{array}{c}
S_{1}^{(3)} \\
S_{2}^{(3)}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{3}{2}\right\rfloor 0 s & \left\lfloor\frac{3+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{3}{2}\right\rfloor 1 s & \left\lfloor\frac{3+1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times 3}=\left[\begin{array}{lll}
0 & 1 & 1 \\
1 & 0 & 0
\end{array}\right]_{2 \times 3}
$$

2. Size of basic matrix of $W_{L}=2$ is defined as $2 \times 2$ and it is created as

$$
M_{W_{L}}=\left[\begin{array}{c}
S_{1}^{(2)} \\
S_{2}^{(2)}
\end{array}\right]=\left[\begin{array}{cc}
\left\lfloor\frac{2}{2}\right\rfloor 0 s & \left\lfloor\frac{2+1}{2}\right\rfloor 1 s \\
\left\lfloor\frac{2}{2}\right\rfloor 1 s & \left\lfloor\frac{2+1}{2}\right\rfloor 0 s
\end{array}\right]_{2 \times 2}=\left[\begin{array}{ll}
0 & 1 \\
1 & 0
\end{array}\right]_{2 \times 2} .
$$

3. $M_{W_{H}}$ is repeated $N_{H}+1=4$ times as

$$
U=\left[\begin{array}{cccc}
011 & . . & . . & . . \\
100 & 011 & . . & . . \\
. . & 100 & 011 & . . \\
. . & . . & 100 & 011 \\
. . & . . & . . & 100
\end{array}\right]
$$

4. Find $R_{W_{H}}=1-1=0$
5. $M_{W_{L}}$ is repeated $N_{L}=3$ times as

$$
U=\left[\begin{array}{ccccccc}
011 & . . & . . & . . & & & \\
100 & 011 & . . & . . & & & \\
. . & 100 & 011 & . . & & & \\
. . & . . & 100 & 011 & & & \\
. . & . . & . . & 100 & 01 & & \\
. . & . . & . . & . . & 10 & 01 & \\
. . & . . & . . & . . & . . & 10 & 01 \\
. . & . . & . . & . . & . . & . . & 10
\end{array}\right] .
$$

6. First and last row of $U$ matrix is removed.

$$
U=\left[\begin{array}{ccccccc}
100 & 011 & . . & . . & & & \\
. . & 100 & 011 & . . & & & \\
. . & . . & 100 & 011 & & & \\
. . & . . & . . & 100 & 01 & . . & . . \\
. . & . . & . . & . . & 10 & 01 & . . \\
. . & . . & . . & . . & . . & 10 & 01
\end{array}\right]
$$

7. Empty spaces are filled with zeros.

$$
U=\left[\begin{array}{lllllllll}
1 & 00 & 011 & 000 & 000 & & & & \\
0 & 00 & 100 & 011 & 000 & & & & \\
0 & 00 & 000 & 100 & 011 & & & & \\
0 & 00 & 000 & 000 & 100 & 01 & 00 & 0 & 0 \\
0 & 00 & 000 & 000 & 000 & 10 & 01 & 0 & 0 \\
0 & 00 & 000 & 000 & 00 & 00 & 10 & 0 & 1
\end{array}\right]
$$

8. Remove all columns which have only 0 s from $U$. Above matrix contains $\left\lfloor\frac{W_{M}+1}{2}\right\rfloor 0 s=\left\lfloor\frac{3+1}{2}\right\rfloor=2$ columns of 0 s towards left side and $\left\lfloor\frac{W_{1}}{2}\right\rfloor 0 s=$ $\left\lfloor\frac{2}{2}\right\rfloor=1$ column of 0 s towards right side.

$$
U=\left[\begin{array}{ccccccc}
1 & 011 & 000 & 000 & & & \\
0 & 100 & 011 & 000 & & & \\
0 & 000 & 100 & 011 & & & \\
0 & 000 & 000 & 100 & 01 & 00 & 0 \\
0 & 000 & 000 & 000 & 10 & 01 & 0 \\
0 & 000 & 000 & 00 & 00 & 10 & 1
\end{array}\right]
$$

9. Code lengths are $L_{W_{H}}=W_{M} *\left(N_{W_{M}}+1\right)+R_{W_{M}}-\left\lfloor\frac{W_{M}+1}{2}\right\rfloor=3 *(3+$ 1) $-2=10$ and $L_{W_{L}}=L_{W_{H}}+W_{L} *\left(N_{W_{L}}\right)-\left\lfloor\frac{W_{L}}{2}\right\rfloor=10+2 *(3)-1=15$. Total code length used by code is 15 .

### 6.4 Performance analysis

Performance metric evaluated for analysis is $B E R$. Let $F_{C}(j)$ be the $j$ th component of the $C$ th proposed code. Correlation function is given as
$F_{X}(j)=\sum_{j=1}^{L_{n}}\left(F_{C}(j) \cdot F_{Z}(j)\right)=\left\{\begin{array}{ccc}W_{i} & C=Z & \text { same user with same weight } \\ 0 & C \neq Z & \text { other users with same weight } \\ 0 & C \neq Z & \text { other users with different weight }\end{array}\right.$

The variance of photocurrent due to the detection of an ideally unpolarized thermal light, which is generated by spontaneous emission, can be written as shown in Eq. (2.10).

The $W_{i}$ unique wavelengths are incident upon a photo detector. The coherence time of a thermal source is given in Eq. (2.9).

The PSD of optical signals at receiver is given in Eq. (4.14).

### 6.4.1 CW-ZCCC BER analysis

Filtered wavelengths are incident upon the input of photodiode of $C$ th receiver. For one bit duration, total power at $C$ th receiver for constant weight is calculated as

$$
\begin{gather*}
\int_{0}^{\infty} G(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N} d_{C} \sum_{j=1}^{L} F_{C}(j) F_{X}(j)\left\{u\left[\frac{\Delta v}{L}\right]\right\}\right] d v  \tag{6.17}\\
=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L} \sum_{k=1}^{N} d_{C} \sum_{j=1}^{L} F_{C}(j) F_{X}(j) \tag{6.18}
\end{gather*}
$$

For CW-ZCCC, the total code length $L_{n}$ is denoted as $L$ and $W_{i}$ becomes $W$ due to constant weight. Applying the correlation property from Eq. (6.16) for same weight condition in Eq. (6.18) gives

$$
\begin{equation*}
\int_{0}^{\infty} G(v) d v=\frac{P_{s r} W}{L} \tag{6.19}
\end{equation*}
$$

The photo current created due to incident optical power at photo diode, is written as

$$
\begin{equation*}
I=\mathcal{R} \int_{0}^{\infty} G(v) d v \tag{6.20}
\end{equation*}
$$

The resultant photo current from Eq. (6.20) is obtained by putting the value from Eq. (6.19) as

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r} W}{L} \tag{6.21}
\end{equation*}
$$

From Eq. (6.21), shot noise is calculated by putting the values of $I$ in

Eq. (2.10) as

$$
\begin{equation*}
\left\langle I_{s h o t}^{2}\right\rangle=2 e B \mathcal{R}\left(\frac{P_{s r} W}{L}\right) \tag{6.22}
\end{equation*}
$$

The PIIN power is given as

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=I^{2} B \tau_{c}=B \mathcal{R}^{2} \int_{0}^{\infty} G^{2}(v) d v \tag{6.23}
\end{equation*}
$$

The approximation is used as per the Eq. (3.19) and by substituting the values in Eq. (6.23) from Eqs. (6.17), PIIN is

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2} N W^{2}}{L^{2} \Delta v} \tag{6.24}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ is given as:

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2} N W^{2}}{L^{2} \Delta v}+2 e B \mathcal{R}\left[\frac{P_{s r} W}{L}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{6.25}
\end{equation*}
$$

Let at any time, the probability of transmitting bit 1 for each user is half, Eq. (6.26) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2} N W^{2}}{2 L^{2} \Delta v}+e B \mathcal{R}\left[\frac{P_{s r} W}{L}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{6.26}
\end{equation*}
$$

The $S N R$ is calculated on substituting Eqs. (6.21), (6.26) in Eq. as

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s s} W}{L}\right)^{2}}{\frac{B \mathcal{R}^{2} P_{S_{r}}^{2} N W^{2}}{2 L^{2} \Delta v}+e B \mathcal{R}\left[\frac{P_{s r} W}{L_{n}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}}} \tag{6.27}
\end{equation*}
$$

The $B E R$ using Gaussian approximation from $S N R$ is expressed as given in Eq. (2.31).

### 6.4.2 VW-ZCCC BER analysis

For one bit duration, total power at $C$ th receiver for variable weight is calculated as

$$
\begin{gather*}
\int_{0}^{\infty} G(v) d v=\int_{0}^{\infty}\left[\frac{P_{s r}}{\Delta v} \sum_{k=1}^{N} d_{C} \sum_{j=1}^{L_{n}} F_{C}(j) F_{X}(j)\left\{u\left[\frac{\Delta v}{L_{n}}\right]\right\}\right] d v  \tag{6.28}\\
=\frac{P_{s r}}{\Delta v} \frac{\Delta v}{L_{n}} \sum_{k=1}^{N} d_{C} \sum_{j=1}^{L_{n}} F_{C}(j) F_{X}(j) \tag{6.29}
\end{gather*}
$$

Applying the correlation property from Eq. (6.16) in Eq. (6.29) gives

$$
\begin{equation*}
\int_{0}^{\infty} G(v) d v=\frac{P_{s r} W_{i}}{L_{n}} \tag{6.30}
\end{equation*}
$$

The photo current created due to incident optical power at photo diode, is written as

$$
\begin{equation*}
I=\mathcal{R} \int_{0}^{\infty} G(v) d v \tag{6.31}
\end{equation*}
$$

The resultant photo current from Eq. (6.31) is obtained by putting the value from Eq. (6.30) as

$$
\begin{equation*}
I=\frac{\mathcal{R} P_{s r} W_{i}}{L_{n}} \tag{6.32}
\end{equation*}
$$

From Eq. (6.32), shot noise is calculated by putting the values of $I$ in Eq. (3.17) as

$$
\begin{equation*}
\left\langle I_{\text {shot }}^{2}\right\rangle=2 e B \mathcal{R}\left(\frac{P_{s r} W_{i}}{L_{n}}\right) \tag{6.33}
\end{equation*}
$$

The PIIN nosie power is given as

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=I^{2} B \tau_{c}=B \mathcal{R}^{2} \int_{0}^{\infty} G^{2}(v) d v \tag{6.34}
\end{equation*}
$$

The total number of users at a given time is the summation of users with different weights that coexist in a single system [42], denoted by

$$
\begin{equation*}
\sum_{h=1}^{N_{\max }} C_{h}=\frac{1}{L_{T}} \sum_{i=1}^{N} N_{W_{i}} W_{i} . \tag{6.35}
\end{equation*}
$$

By substituting the values in Eq. (6.34) from Eqs. (6.17), PIIN noise is

$$
\begin{equation*}
\left\langle I_{P I I N}^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2}}{L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\text {max }}} N_{W_{i}} W_{i}\left[W_{i}\right] \tag{6.36}
\end{equation*}
$$

Noise power, $\left\langle I^{2}\right\rangle$ is given as:

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2}}{L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\max }} N_{W_{i}} W_{i}\left[W_{i}\right]+2 e B \mathcal{R}\left[\frac{P_{s r} W_{i}}{L_{n}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{6.37}
\end{equation*}
$$

Let at any time, the probability of transmitting bit 1 for each user is half, Eq. (6.37) leads to

$$
\begin{equation*}
\left\langle I^{2}\right\rangle=\frac{B \mathcal{R}^{2} P_{s r}^{2}}{2 L_{T}^{2} \Delta v} \sum_{i=1}^{N_{\max }} N_{W_{i}} W_{i}\left[W_{i}\right]+e B \mathcal{R}\left[\frac{P_{s r} W_{i}}{L_{n}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}} \tag{6.38}
\end{equation*}
$$

Substituting Eqs. (6.32), (6.38) in Eq. (2.29), $S N R$ is expressed as

$$
\begin{equation*}
S N R=\frac{\left(\frac{\mathcal{R} P_{s s} W_{i}}{L}\right)^{2}}{\frac{B \mathcal{R}^{2} P_{s r}^{2}}{2 L_{T}^{2} \Delta v} \sum_{i=1}^{N_{m a x}} N_{W_{i}} W_{i}\left[W_{i}\right]+e B \mathcal{R}\left[\frac{P_{s r} W_{i}}{L_{n}}\right]+\frac{4 K_{b} T_{n} B}{R_{L}}} \tag{6.39}
\end{equation*}
$$

The $B E R$ is computed as given in Eq. (2.31).


Figure 6.1: Comparison of ZCC, KS, EDW, RD, MS, MDW and proposed codes for $B E R$ versus number of users.

### 6.5 Numerical Results

Proposed code is compared with the previously reported ZCC Code, KS [42], RD [87], MS [47], MDW [59] and EDW [88] codes in Figure 6.1. KS code [42] was reported with variable weight code construction. Its crosscorrelation is given by $\left(\lambda_{c} \leq 1\right)$. It was designed with even weights only. EDW code [88] was designed with odd weights only and it was used for multirate transmission. MDW code [30] was designed with even weights only. MS code was designed for variable number of users in basic code with fixed weight. All above described codes are using mapping technique to provide codes for greater number of users. RD code [87] divide code sequence into two parts (code, and data) segments. Code segment exhibits ZCC property. Proposed code does not use the mapping technique to provide codes. The parameters used for numerical comparison are listed in Table 2.2.

Figure 6.1 is plotted for $B E R$ versus number of users. Proposed code is constructed with weight 4 and 100 users. KS code, ZCCC, RD code, MS code and EDW code are designed with weights 6, 4, 4, 4 and 3 respectively


Figure 6.2: Comparison between the Figure 6.3: Comparison between the previously reported ZCC code and pro- previously reported ZCC code and proposed ZCCC for constant weight (CW). posed ZCCC for variable weight (VW) without PIIN consideration.
with 100 users each. Proposed code has almost same $B E R$ as compare to ZCCC without PIIN consideration for weight 4. That is because of same zero cross-correlation, code length, weight, noise consideration, and number of users. All codes except ZCCC give higher $B E R$ as compared to proposed code $(W=4)$. That is due to cross-correlation property of these codes. The number of users for EDW code ( $W=3$ ), KS code ( $W=6$ ), MS code $(W=4)$, RD code $(W=4)$ and proposed ZCCC $(W=4)$ are 41, 54, 47, 48 and 64 respectively at $B E R$ of $10^{-10}$ with PIIN consideration. The number of users for proposed code and ZCCC is 83 users at $10^{-10}$ without PIIN consideration.

Comparison between the previously reported ZCC code and proposed ZCCC is shown in Figures 6.2 and 6.3. Figure 6.2 shows variation of code length as a function of number of users. Reported ZCC code used the mapping technique to assign codes for higher number of users. Variation of code length depends on basic matrix size which is determined by code weight. As weight is increased, size of basic matrix increases which leads to higher step size, whereas proposed ZCCC has a linear increment of code length.



Figure 6.4: Comparison of $B E R$ ver- Figure 6.5: Comparison of $B E R$ versus number of users on varying $N_{H}$ of sus number of users on varying $N_{L}$ of weight $\left(W_{H}\right)$ with PIIN consideration. weight $\left(W_{L}\right)$ with PIIN consideration.

Reported ZCC code used code transformation technique, which converts the lower weight code to higher weight code [36], whereas proposed ZCCC has no restriction to construct codes of any weight. Proposed ZCCC require less number of filtering elements compare to reported ZCC code. For reported ZCC code, numbers of filtering elements are equal to number of weight. Proposed ZCCC requires two filtering elements irrespective to weight.

Figure 6.3 shows the $B E R$ comparison of ZCC code and VW ZCCC as a function of code length without PIIN consideration. $\left(W_{H}\right)$ and $\left(W_{L}\right)$ are used to indicate higher weight, and lower weight respectively. $N_{H}$ and $N_{L}$ represent number of users for higher weight $\left(W_{H}\right)$ and lower weight $\left(W_{L}\right)$ respectively. The values of $N_{H}$ and $N_{L}$ are 50 for each weight. Total number of users are 100 for VW-ZCCC. For reported ZCC code, weight and number of users are 4 and 100 respectively. VW-ZCCC and ZCC code are required 350 and 400 code lengths respectively. VW ZCCC requires less code length compare to ZCC code. It is due to variable weight code construction. Variable $B E R$ is obtained by using VW ZCCC compare to ZCC code.

Figures 6.4 and 6.5 illustrate the $B E R$ versus number of users with PIIN


Figure 6.6: Comparison of $B E R$ versus number of users for three different weights with PIIN consideration.
consideration. The combination of weights $\left(W_{H}=7, W_{L}=6\right)$ are chosen for Figs. 6.4 and 6.5.

For Fig. 6.4, number of users $N_{L}$ for $W_{L}$ are set to 50 users. The number of users $N_{H}$ is varied and it is set to 50,45 and 40 users. Higher number of users leads to longer code length and vice versa. Change in code length affect the $B E R$ of system. On increasing / decreasing the value of $N_{H}, B E R$ increases / decreases. The variation in $B E R$ is due to different weights which further change the code length. Results indicate lowest weight codes have highest $B E R$ and highest weight codes have lowest $B E R$.

For Fig. 6.5, number of users $N_{L}$ is varied and it is set to 50,45 and 40 users. The number of users $N_{H}$ is set to 50 users. As the number of users of $N_{L}$ decreases, code length decreases which tends to decrease $B E R$. The $W_{L}$ does not affect the code length of $W_{H}$ but the total code length is decreased thus $B E R$ of $W_{H}$ is decreased.

Figure 6.6 is plotted between the $B E R$ versus number of users with PIIN consideration. The $\left(W_{H}\right),\left(W_{M}\right)$ and $\left(W_{L}\right)$ are used to indicate different


Figure 6.7: Simulation setup of encoder with optical fiber using OptiSystem 13 . is designed for 4 users of weight 3 .
weights as higher weight, medium weight and lower weight respectively. The combination of weights $\left(W_{H}=7, W_{M}=6, W_{L}=5\right)$ is chosen. The $N_{H}$, $N_{M}$ and $N_{L}$ are denoted as number of users for higher weight $\left(W_{H}\right)$, medium weight ( $W_{M}$ ) and lower weight ( $W_{L}$ ) respectively. The number of users are set to 30 users for each weight. $N_{L}$ effect the total code length not the code length of $N_{H}$ and $N_{M}$.

On changing $N_{H}$, code lengths of all lower weight codes are changed. On the other hand, changing $N_{L}$, effects its own code length and total code length, but does not effect codes of other weights. Different weights provide variable $B E R$. Resultant code is suitable for multimedia service.

### 6.6 Simulation Setup and Results

The simulation setup with LED as a broadband light source is shown in Figs.
6.7 and 6.8, using OptiSystem 13.


Figure 6.8: Simulation setup of decoder with optical fiber using OptiSystem 13 . is designed for 4 users of weight 3 .

Simulation setup for proposed ZCCC is designed for 4 users of weight 3 . Data rate for simulation is set to 622 Mbps . Spectral width is set to .8 nm for each chip. The transmitter side consists of five components: a pseudo random bit sequence (PRBS) generator, a non-return-zero (NRZ) pulse generator, LED with bias generator, WDM demux and mux (for filtering wavelength), and an external modulator. The simulation parameters of LED are set as wavelength of 1550 nm , bandwidth of $3.75 \mathrm{THz}(30 \mathrm{~nm})$, external quantum efficiency is 0.05 , and transmitted Power is -10 dBm . Spectrum slicing of LED is elaborated as per [37]. The external intensity modulators used are MachZehnder modulators. All signals from all users are combined and launched into a single fiber. Fiber length is chosen to be 9 Km with dispersion of $16.75 \mathrm{ps} / \mathrm{nm}-\mathrm{km}$, and attenuation of $0.2 d B / \mathrm{km}$.

Direct detection technique is used to detect signals. This technique requires only one photodiode to detect unique wavelengths of each user. At recevier, the incoming signal was split and sent to wavelength mux to detect
C H A P TER 6. $C W$ AND $V W Z C C C$
$\qquad$ BER Analyzer_2


Figure 6.9: The comparison of Q factors between reported ZCC code and proposed ZCCC.
required wavelengths. Photodiode parameters are set as dark current of $5 n A$, responsivity of $1 A / W$, thermal noise of $100 \times 10^{-24} W / H z$, and with gain of 10.

Simulation setup for previously reported ZCC code is designed for 4 users of weight 3 . The minimum possible users for weight 3 is 4 . Reported ZCC code has dependence on basic matrix. Proposed ZCCC has not basic matrix limitation. Simulation setup for reported ZCC code has same parameters values as defined for setup in Figs. 6.7 and 6.8. The trasmitter side has same components as per shown in Fig. 6.7. Q factor and $B E R$ of 9.22 and $7.64 \times 10^{-21}$ are achieved by proposed ZCCC. Q factor and $B E R$ of 6.99 and $7.77 \times 10^{-13}$ are achieved by reported ZCC code. The comparison of Q factors between reported ZCC code and proposed ZCCC are shown in Fig. ??.

### 6.7 Summary

ZCCC is proposed without mapping. Code algorithm is designed with any integer value of weight for any number of users. Algorithm is explained for both constant and variable weight code construction.

CW ZCCC is compared with reported ZCC code. Proposed ZCCC construct any weight code without any information about lower weight codes. It construct the code without mapping. It has a linear increase in code length. Variable weight (VW) codes give different quality of service, and are suitable, and useful for multimedia applications. Construction of code for variable weight is begins with the highest weight. On changing number of users of highest weight, code length of all lower weight codes are changed. On the other hand, changing number of users of lower weight, effects its own code length and total code length, but does not effect codes of other weights. The variation of weights provides different $B E R$ and code length.

## Conclusions and Future <br> Directions

### 7.1 Concluding Remarks

The thesis proposes some new algorithms to construct codes for SAC-OCDMA systems. The main purpose of algorithms are to support higher cardinality with better performance, to simplify code construction with variety of code sets and, good properties like auto-correlation, cross-correlation and to support multimedia applications and fill the gaps in reported code constructions.

The outcomes obtained from these studies are summarized below:

### 7.1.1 DW code families for SAC-OCDMA systems

Chapter 2 presents the review on code construction algorithms of 1D codes DW code families and a gap between the reported works. Using reported

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codes, odd weight construction of KS code and 2D code construction from 1D DW code families are proposed.

The odd weight code construction for KS code is a combination of previously proposed KS code (for even weight) and identity matrix. It provides an extension of KS code by implementing for all weight construction. Application of proposed KS code for FSO channel and multi media service can be explored. The 2D code is proposed which is constructed using 1D DW code families for weight greater than 1. The proposed 2D code provides higher cardinality at lower $B E R$ on comparing with 1D code. Hence, it provides a solution for limited bandwidth of BBS. On comparing with other 2D codes, proposed 2D code has lower $B E R$. $B E R$ is decreased as $h$ is maximized and $g$ is minimized. Hence, a solution is provided by incresing the dimensions of code to enchance number of users, and lower $B E R$.

### 7.1.2 Generalized Optical Code construction for EDW and MDW like Codes without mapping

Chapter 3 introduces an algorithm named as Generalized Optical Code construction for EDW and MDW like Codes without mapping. The $B E R$ analysis is same for all weights greater than 2. Comparison with EDW and MDW codes shows proposed code is having lower $B E R$. At $B E R$ of $10^{-9}$, number of users are 61 and 58 for $W=3$ and $W=4$ respectively for generalized code. The number of users for EDW $(W=3)$ and MDW $(W=4)$ are 34 and 61 respectively. The variation of results are due to difference in code length which depends on the number of users and its dependency on mapping for EDW and MDW which affects the $B E R$ performance. Compared to the BD , DD does not require power splitter, two photodiodes and subtractor at decoder of each user. Due to the use of less components, the cost of the

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system is lower $[56,85]$.

### 7.1.3 VW code construction using Generalized code

In Chapter 4, VW algorithm based on Chapter 3 is proposed without mapping. Proposed code requires two filtering elements irrespective of weight. The variation of weights provides different $B E R$. The lowest weight codes have highest $B E R$ and highest weight codes have lowest $B E R$. It is observed that supportable number of users for higher weight, at $B E R$ of $10^{-9}$ (data) are 28, 33 and 35 for RD code, KS code, and VW code respectively using BD. Supportable number of users for lower weight, at $B E R$ of $10^{-4}$ (voice) are 23, 31 and 37 for RD code, KS code, and VW code respectively using BD . Results show that code is suitable for multimedia application. By using DD technique, receiver is designed with less complexity and its cost is reduced along with better performance. Figure 4.6 illustrates the $B E R$ (PIIN, Shot and thermal noise) versus received power using balanced detection for $W_{H}=6, W_{M}=5, W_{L}=3$ with 25 users for each weight. $B E R$ of all users decreases with the increase of weight and received power. The application of proposed VW code to support different services, for average received power of -20 dBm has acceptable performance. It is found that proposed VW code gives comparable and better performance than Generalized Optical Code construction for Enhanced and Modified Double Weight code (CW and CL construction). That is due to lower code length of variable weight codes.

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### 7.1.4 A new code construction algorithm based on DW

 CodesA new and single code construction algorithm with mapping is proposed for DW code families in Chapter 5. The code design has several advantages such as simplicity of code construction, the weight of any positive number can be used for the code design and variety of code set for different code length and weight. Code length increment of EDW code is differ from proposed code. The difference is shown in Fig. 5.2, for weight $(W=3)$ and basic matrix of ( $N_{B}=3, L_{B}=6$ ). Difference in the length is due to different techniques used to calculate code length $(L)$ for N users. For EDW, it involve a sine relation between $L$ and $N$ [31]. Proposed code follows constant variation of code length defined in Eq. 5.27. These code length variations effect the $B E R$ performance of codes which depend on $N$ and $L$.

A 2D code is proposed for SAC-OCDMA systems. The code is having a low value of IPCC for spectral dimension and orthogonal in spatial dimension. In comparison with 1D code, it offers greater number of users along with better $B E R$ performance. On comparing with hybrid code, it gives lower $B E R$.

### 7.1.5 Development of ZCCC for Constant and Variable Weight

An algorithm is proposed for CW and VW using zero cross correlation property without mapping in Chapter 6. Code algorithm is designed with any integer value of weight for any number of users. Comparison between the previously reported ZCC code and proposed ZCCC is shown in Figures 6.2 and 6.3. Reported ZCC code used the mapping technique to assign codes

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for higher number of users. Variation of code length depends on basic matrix size which is determined by code weight. As weight is increased, size of basic matrix increases which leads to higher step size, whereas proposed ZCCC has a linear increment of code length. Reported ZCC code used code transformation technique, which converts the lower weight code to higher weight code [36], whereas proposed ZCCC has no restriction to construct codes of any weight. Proposed ZCCC require less number of filtering elements compare to reported ZCC code. For reported ZCC code, number of filtering elements are equal to number of weight. Proposed ZCCC require two filtering elements irrespective to weight.

Construction of code for variable weight is begins with the highest weight. On changing number of users of highest weight, code length of all lower weight codes are changed. On the other hand, changing number of users of lower weight, effects its own code length and total code length, but does not effect codes of other weights. The variation of weights provides different $B E R$ and code length. Results indicate that lowest weight codes have highest $B E R$ and highest weight codes have lowest $B E R$. Resultan, code is suitable for multimedia service.

### 7.2 Scope for Further Study

Proposed algorithms are analyzed by taking the effects of PIIN, shot noise and thermal noise. Therefore, the performance of codes can be analyzed by considering the other noise. For mathematical simplification, some assumptions are taken such as LED spectrum is flat. But, spectrum has a Gaussian shape, means different wavelengths on spectrum have different amplitude. So, to analyse $B E R$ some practical consideration is may be taken for further

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extension to $B E R$ equation. Optical power budget analysis is also estimated due to various components in systems as an further extension of work. Extension of codes to design it in multi-dimension, to enhance cardinality by reducing $B E R$. Lower and upper bounds of these codes are also investigated. The experimental and simulation results are also demonstrated. Application of these codes can be tested for other domain of OCDMA, wireless optical systems, Free Space Optics, and Visible Light Communication.

Also, since spectrum slicing plays an important role in encoding of the spectrum, new methods can be studied for use in SAC-OCDMA systems. The analysis of encoder/decoder circuit with suitable optical devices can be introduced to reduce the PIIN and to improve the system performance.

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# Publications from the Thesis Work 

## Journals (Accepted/Communicated)

1. Soma Kumawat, M. Ravi Kumar, "Generalized Optical Code construction for Enhanced and Modified Double Weight like Codes without mapping for SAC-OCDMA systems," Optical Fiber Technology, vol. 30, pp. 72-80, 2016.
2. Soma Kumawat, M. Ravi Kumar, "Development of ZCCC for multimedia service using SAC-OCDMA systems," Optical Fiber Technology, vol. 39, pp. 12-20, 2017.
3. Soma Kumawat, M. Ravi Kumar, "Design of Variable Weight code for multimedia service in SAC-OCDMA systems," IET Optoelectronics, vol. 12 (2), pp. 56-64, 2018.

## Conference Proceedings

1. Soma Kumawat, M. Ravi Kumar, "Design and Analysis of Different Decoders for SAC-OCDMA Systems.," Proceedings of the International Conference on Recent Cognizance in Wireless Communication \& Image Processing (ICRCWIP-2014), Springer, New Delhi DOI:doi.org/10.1007/978-81-322-2638-3 ${ }_{49}$.
2. Soma Kumawat, M. Ravi Kumar, "Analysis of Diagonal Eigenvalue Unity (DEU) code for Spectral Amplitude Coding OCDMA systems using Direct Detection technique," 2015 International Conference on Microwave, Optical and Communication Engineering (ICMOCE), Bhubaneswar, 2015, pp. 45-48. DOI: 10.1109/ICMOCE.2015.7489687
3. Soma Kumawat, M. Ravi Kumar, "A new code construction algorithm based on Double Weight codes for SAC-OCDMA systems," 2017 International Conference on Computer, Communications and Electronics (Comptelix), Jaipur, 2017, pp. 1-6. DOI: 10.1109/COMPTELIX.2017.8003927.
4. Soma Kumawat, M. Ravi Kumar, "A new technique to construct Zero cross correlation code for SAC-OCDMA," Optical and Wireless Technologies (OWT), Jaipur, 2017. DOI: 10.1007/978-981-10-7395-3 ${ }_{4}$.
5. Soma Kumawat, M. Ravi Kumar, "2D code construction using DW code families for SAC-OCDMA systems," TENCON, Malaysia, 2017. DOI: 10.1109/TENCON.2017.8228273
6. Soma Kumawat, M. Ravi Kumar, "A review on code families for a SAC-OCDMA systems," Optical and Wireless Technologies (OWT), Jaipur, 2018.
7. Soma Kumawat, M. Ravi Kumar, "2D Spectral/Spatial code construction for SAC-OCDMA system," ICRAIE, Jaipur, 2018, communicated.

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